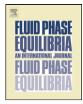
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Measurement of ternary polymer/solvent equilibrium data by vapor-phase infrared spectroscopy

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A R T I C L E I N F O

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ABSTRACT

Vapor–liquid equilibrium (VLE) data for binary toluene/PVAC, methanol/PVAC and ternary toluene/methanol/PVAC systems have been measured at 100 °C by using vapor-phase infrared spectroscopy. Binary data have been compared with literature data measured by different experimental techniques and agreement between our measurements and others was found to be good. The ternary VLE data indicate that the solubility of methanol in PVAC is not influenced by the presence of toluene, while the solubility of toluene is lowered due to presence of methanol. To predict ternary VLE data, the Entropic free volume and Kannan free volume models and the Flory-Huggins theory were used. The predictive abilities of Flory-Huggins theory and the Kannan free volume model are similar and better than that of the Entropic free volume model.

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1. Introduction

Knowledge of vapor liquid equilibrium (VLE) of polymer solutions is essential in the efficient design and optimization of industrial polymer processing unit operations. A few examples include removal of solvents, unreacted monomers and other residues at the end of polymerization, drying of polymer solutions, formulations of paints and coatings and separation of organic mixtures and gases by polymeric membranes.

VLE data for various binary polymer solvent mixtures exist in the literature, however, in some applications, it is necessary to dissolve the polymer in mixed solvents and only very few data are available on VLE of mixed solvents polymer systems. The main reason for the lack of multicomponent equilibrium studies is the difficulty in determining the compositions of both liquid and vapor phases. Combined with a material balance, gas chromatography was the first method used by Katayama and co-workers to measure the ternary VLE data of mixed solvents polymer systems [1,2]. The technique was found to be laborious and difficult to use at elevated temperatures. Therefore, Bonner and co-workers developed a perturbation chromatography technique [3,4] which was also adopted by Glover and his group in measuring ternary VLE data for different polymer solvents systems [3–8]. More recently, the classical gravimetric sorption technique using either quartz spring weigh-

ing [9,10] or a magnetic suspension balance [11] was modified for acquiring sorption data of mixed solvents dissolved in the polymer.

A new analytical technique based on vapor-phase infrared spectroscopy has been developed by Zielinski et al. [12]. The IR technique allows to determine entire sorption isotherms in parallel and facilitates the data acquisition at a much faster rate than conventional methods. In standard gravimetric and volumetric sorption methods, equilibration time to measure each data point on the isotherm can vary from a few hours to 1 day depending on the temperature and sample thickness. In addition, experiments should be conducted in series resulting in a long time to generate the full isotherm. The pressure attainable in most conventional gravimetric and volumetric sorption apparatuses is usually limited to 1 atm. In the case of the IR technique, the upper pressure limit depends only on the quality of the seal made in capping the sample vials.

Zielinski et al. [12] applied the IR technique to measure binary sorption data for the toluene/polyvinyl acetate and methanol/polyvinyl acetate (PVAC) systems at 100 °C, however, they indicated that the method can also be used to measure VLE data in polymeric systems containing multiple solvents if the IR peaks of the solvents can be separated from each other. In this study, we employed the IR technique to measure ternary sorption data for the toluene/methanol/polyvinyl acetate system at 100 °C. The accuracy of our measurements has been confirmed by comparing the toluene/polyvinyl acetate and methanol/polyvinyl acetate data with literature data collected by other experimental techniques. The ternary sorption data were correlated with the Flory-Huggins theory and the Entropic and Kannan free volume models.

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2. Materials

Toluene and methanol with the purities of 99.8% were obtained from Riedel and PVAC (molecular weight: 113,000 g/mol; density: 1.19 g/cm³) was supplied from Aldrich. The 20 ml headspace gas chromatography (GC) vials were purchased from Agilent.

3. Method

The basic principles of the IR technique used in this study are given by Zielinski et al. [12]. Briefly, a certain amount of PVAC dried at 100 °C for 24 h is put into a GC vial and a known amount of solvent is injected into the vial which is then sealed with an aluminium crimpcap teflon phased septa with a diameter of 20 mm. A teflon disk instead of a conventional septum is used to minimize the experimental error associated with the sorption of solvents into the rubber septum. In order to achieve vapor-liquid equilibria, the sample cell is placed into a temperature-controlled oven. Immediately after removal, it is then inserted into the top of a heater assembly to conduct in situ IR measurement at the specified temperature. A heating assembly made of an aluminium block is selected because of its high thermal conductivity. A schematic illustration of the heater assembly is given in Fig. 1. The inner diameter of the block softly touches the surface of the GC vials so that the heat can be homogenously conducted along the vial. The electrical heater is placed at the bottom of the assembly and it is connected to a PID temperature controller with an accuracy of ± 0.5 °C. To minimize the heat loss during analysis, the assembly is covered with a polyurethane insulating material. Two holes at the lateral surfaces of the assembly allow the IR beam to pass through the GC vial. Spectra were obtained at 4 cm⁻¹ resolution using a Digilab Excalibur Series, FTS 3000MX FT-IR instrument equipped with a deuterated triglycine sulfate (DTGS) detector. In order to increase signal to noise ratio, the number of scans was set to 128 for all runs.

To minimize the contribution of the systematic errors caused by sorption of the solvents in the GC vials during analysis of the vapor-phase composition, three important parameters were investigated: position and background of GC vials, sample preparation and temperature of the assembly. While rotating the GC vial does not give any difference in the spectra, variations are observed in the background spectrums between different vials. Therefore, through-

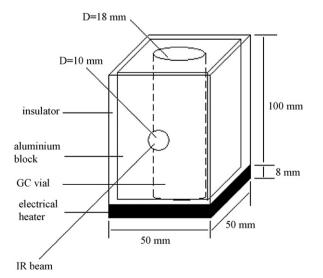


Fig. 1. Schematic representation of the heating assembly used in the FTIR sample chamber.

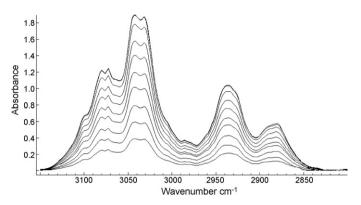


Fig. 2. FT-IR spectra used for the calibration curve of toluene at 100 °C. Spectra correspond to 10–50 μ l of toluene in increments of 5 μ l.

out the study background spectrums at the specified temperature $(100 \,^\circ \text{C})$ were obtained for each empty GC vials. All the samples were prepared in a nitrogen glovebox due to sensitivity of the IR technique to water and CO₂.

4. Analysis method

Quantitative analysis of the IR spectrum were obtained by first constructing a calibration curve. For that purpose, known amounts of methanol and toluene were injected into empty GC vials using 10–100 µl syringes. The maximum amount of solvents introduced was 55 µl for toluene and 100 µl for methanol. These values correspond to saturation volumes at 100 °C above which condensation of the solvents was observed. The change in absorbance intensities of toluene and methanol with vapor-phase concentrations is illustrated in Figs. 2 and 3, respectively. In these figures, any specific peak of the components can be selected for analyzing the VLE data. Based on the procedure followed by Zielinski et al. [12], we have chosen the 3099.57 cm^{-1} peak for toluene and the 3680.17 cm^{-1} peak for methanol. Figs. 4 and 5 show the calibration curves at 100 °C for toluene and methanol, respectively. By knowing the volume of the vapor phase, the calibration curves were utilized to calculate the mass of the solvents in the vapor phase of the headspace GC vials. While generating the calibration curves, the vapor-phase volume, $V_{\rm g}$, was taken as the total volume of the vial, $V_{\rm T}$, which was determined to be 20.4 cm³. During the analysis of polymer/solvents VLE data, it was calculated by subtracting the volume of the polymer from the total volume of the empty vial. Assuming that there is no volume change on mixing, the volume of the polymer, $V_{\rm p}$, was estimated by summing the volumes of the dry polymer and the solvents

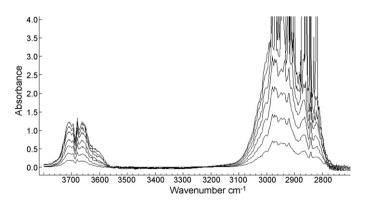


Fig. 3. FT-IR spectra used for the calibration curve of methanol at 100 °C. Spectra correspond to 10–60 μ l of methanol in increments of 10 μ l.

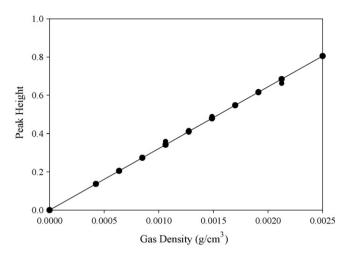


Fig. 4. Calibration curve for the 3099.57 cm $^{-1}$ toluene IR peak with respect to vapor-phase toluene mass density at 100 $^\circ$ C.

absorbed as follows:

$$V_{\rm p} = \frac{m_{\rm pd}}{\rho_{\rm p}} + \frac{m_{\rm 1p}}{\rho_{\rm s1}} + \frac{m_{\rm 2p}}{\rho_{\rm s2}} = V_{\rm T} - V_{\rm g} \tag{1}$$

In Eq. (1), m_{pd} and ρ_p correspond to the mass and the density of pure polymer, respectively, while m_{ip} represents the mass of solvent *i* in the polymer phase and ρ_{si} denotes its pure component density. As shown in Eq. (2), the mass of solvent *i* in the polymer phase was determined from the difference between the total amount of solvent *i* introduced into the system, $m_{Ti} = \rho_i V_{Ti}$, and the mass of solvent *i* remained in the vapor phase:

$$m_{\rm ip} = m_{\rm Ti} - \rho_{\rm gi} V_{\rm g} \tag{2}$$

The vapor-phase concentration of component *i*, ρ_{gi} , required in Eq. (2) was directly obtained from the calibration curve by detecting the vapor-phase signal intensity (H_i) during IR measurements:

$$\rho_{\rm gi} = \frac{H_{\rm i}}{m_{\rm i}} \tag{3}$$

where m_i is the slope of the calibration curve. An expression for the volume of gas phase, V_g , is obtained by combining Eqs. (1) and (2):

$$V_{\rm g} = \frac{V_{\rm T} - \{(m_{\rm pd}/\rho_{\rm p}) + (m_{\rm T1}/\rho_{\rm s1}) + (m_{\rm T2}/\rho_{\rm s2})\}}{1 - (\rho_{\rm g1}/\rho_{\rm s1}) - (\rho_{\rm g2}/\rho_{\rm s2})}$$
(4)

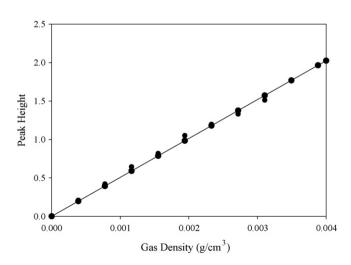


Fig. 5. Calibration curve for the 3680.17 cm $^{-1}$ methanol IR peak with respect to vapor-phase methanol mass density at 100 $^\circ\text{C}.$

In constructing the sorption isotherms, solvent activities (a_i) and volume fractions (ϕ_i) were calculated as follows:

$$a_{i} = \frac{P_{i}}{P_{i}^{o}} \quad \phi_{i} = \frac{m_{ip}/\rho_{si}}{V_{p}} \tag{5}$$

In Eq. (5), the partial pressure of solvent *i*, P_i , was estimated from the ideal gas law:

$$P_i = \frac{\rho_{\rm gi} RT}{M_i} \tag{6}$$

where M_i is the molecular weight of solvent *i*, and the vapor pressure of component *i*, P_i^o , was taken from the literature [13]. The uncertainties in a_i and ϕ_i caused by uncertainties in the experimental measurements were calculated in Appendix A.

5. Prediction of sorption data

To predict the VLE of the toluene/methanol/PVAC system, two purely predictive models (Entropic Free Volume and Kannan Free Volume) and one molecular model (Flory-Huggins) have been used. The free volume models in terms of activity coefficients, γ_i , are of the form [14]:

$$\ln \gamma_i = \ln \gamma_i^{\text{comb} - f\nu} + \ln \gamma_i^{\text{res}}$$
⁽⁷⁾

where the residual contribution, $\ln \gamma_i^{\text{res}}$, is obtained from the UNI-FAC residual term [15] and combinatorial/free volume terms are defined below.

5.1. Entropic free volume model

$$\ln \gamma_i^{\text{comb}-f\nu} = \ln \left(\frac{\phi_i^{f\nu}}{x_i}\right) + 1 - \frac{\phi_i^{f\nu}}{x_i} \tag{8}$$

where ϕ_i^{fv} is the free-volume fraction of component *i*

$$\phi_{i}^{f\nu} = \frac{x_{i}v_{i}^{f\nu}}{\sum_{j}x_{j}v_{j}^{f\nu}}$$
(9)

and x_i is the mole fraction of component *i* and v_i^{fv} is the free volume of component *i* which is calculated by subtracting the van der Waals volume of component *i* from its molar volume.

5.2. Kannan free volume model

$$\ln \gamma_i^{\text{comb}-f\nu} = \ln \gamma_i^{\text{comb}} + \ln \gamma_i^{f\nu} \tag{10}$$

The combinatorial contribution, $\ln \gamma_i^{\text{comb}}$, in Kannan free volume model is obtained from original UNIFAC expansion, while the free volume term is given as follows:

$$\ln \gamma_i^{fv} = \ln \left(\frac{\phi_i^{fv}}{\phi_i^{hc}} \right) + \left(\frac{\phi_i^{hc} - \phi_i^{fv}}{x_i} \right)$$
(11)

The hard-core volume fraction of component *i* is calculated as

$$\phi_i^{\rm hc} = \frac{x_i \nu_i^{\rm hc}}{\sum_j x_j \nu_j^{\rm hc}} \tag{12}$$

and the hard-core volume of component i, v_i^{hc} , is taken to be equal to its van der Waals volume. In the Flory-Huggins theory, the activity

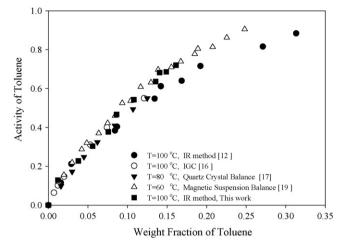


Fig. 6. Comparison of equilibrium sorption data of the toluene/PVAc system measured at 100 $^\circ$ C by the IR technique and with the literature data.

of the solvents in a ternary system of 2 solvents and a polymer (1, solvent 1; 2, solvent 2; 3, polymer) is given by following equations:

$$\ln a_{1} = \ln \phi_{1} + 1 - \phi_{1} - \frac{V_{1}}{V_{2}}\phi_{2} - \frac{V_{1}}{V_{3}}\phi_{3} + (\chi_{12}\phi_{2} + \chi_{13}\phi_{3})(\phi_{2} + \phi_{3}) - \chi_{23}\frac{V_{1}}{V_{2}}\phi_{2}\phi_{3}$$
(13)

$$\ln a_{2} = \ln \phi_{2} + 1 - \phi_{2} - \frac{V_{2}}{V_{1}}\phi_{1} - \frac{V_{2}}{V_{3}}\phi_{3} + \left(\chi_{12}\frac{V_{2}}{V_{1}}\phi_{1} + \chi_{23}\phi_{3}\right)(\phi_{1} + \phi_{3}) - \chi_{13}\frac{V_{2}}{V_{1}}\phi_{1}\phi_{3}$$
(14)

In Eqs. (13) and (14), ϕ_i and V_i represent volume fraction and molar volume of component *i* while χ_{ij} corresponds to interaction parameter between component *i* and *j*.

6. Results and discussion

To illustrate the accuracy of the IR method, we have first measured the VLE data for toluene/PVAC and methanol/PVAC systems at 100 °C and compared them with literature data measured by different groups [11,12,16–19]. Methanol sorption data have also been collected in our laboratories (at 60 °C) by gravimetric sorp-

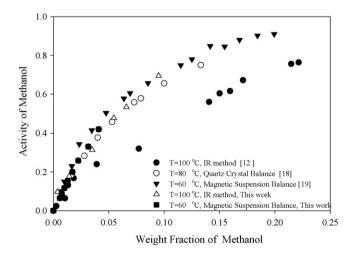


Fig. 7. Comparison of equilibrium sorption data of the methanol/PVAc system measured at 100° C by the IR technique and with the literature data.

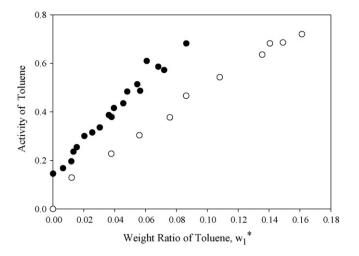


Fig. 8. The change of activity of toluene with respect to its weight ratio in PVAC. Open circles represent data for toluene/PVAC binary system while closed circles represent data for toluene/methanol/PVAC ternary system.

tion using a magnetic suspension balance. The results presented in Figs. 6 and 7 clearly indicate a good agreement between our IR data and those obtained using different experimental techniques. As shown in Fig. 7, methanol solubilities measured by Zielinski et al. [12] using the IR technique are higher than the other data sets and this may be due to difference in molecular weights of the polymers used in different studies. To emphasize the advantage of the IR technique in VLE measurements, it is important to note that most conventional gravimetric sorption devices are limited to 1 atm of pressure, thus, the maximum activity of methanol achievable at 100 °C is about 0.29. On the other hand, the maximum pressure of methanol attained in our measurements was 2.42 atm which allowed to collect the sorption data up to an activity level of around 0.7. The pressure limitation in the IR technique depends on the quality of the cap seal due to the possibility of solvent leakage.

VLE data for toluene (1)/methanol (2)/PVAC (3) system have been measured at 100 °C. To compare the ternary sorption data with those of the corresponding binary systems, the data are presented in terms of the weight ratio of each solvent absorbed in the polymer: $w_i^* = m_{si}/(m_{si} + m_{pd})$ as a function of the corresponding activities in the vapor phase. As illustrated in Figs. 8 and 9, the solubility of methanol in PVAC is not influenced by the presence of

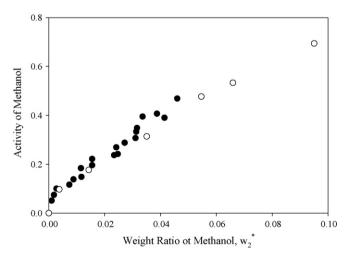


Fig. 9. The change of activity of methanol with respect to its weight ratio in PVAC. Open circles represent data for methanol/PVAC binary system while closed circles represent data for toluene/methanol/PVAC ternary system.

Table 1

The list of molar volumes and Flory-Huggins interaction parameters for the toluene (1)/methanol (2)/PVAC (3) system.

Parameter	Value	
$ \chi_{12} \\ \chi_{13} \\ \chi_{23} \\ V_1 (cm^3/mol) \\ V_2 (cm^3/mol) \\ V_3 (cm^3/mol) $	4.39 ^a 0.705 ^b 1.03 ^b 112.9 [13] 40.5 [13] 94,958 ^c	

^a Calculated from the solubility parameters: $\chi_{12} = (V_1/RT)(\delta_1 - \delta_1)^2$ $\delta_1 = 8.91 (cal/cm^3)^{0.5} [13]; \delta_2 = 14.28 (cal/cm^3)^{0.5} [13].$

^b Regressed from binary VLE data.

^c Calculated from the density and molecular weight of PVAC.

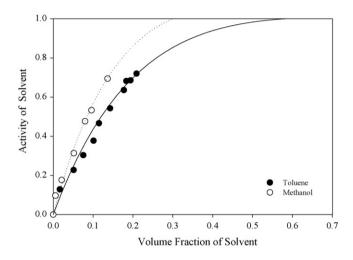


Fig. 10. Equilibrium sorption data for the toluene/PVAC and methanol/PVAC systems measured at 100 °C. The symbols and solid lines represent experimental data and a correlation using the Flory-Huggins model with constant interaction parameter, respectively.

toluene, while the solubility of toluene is lowered due to presence of methanol. The ternary VLE data have been described using the Entropic free volume, Kannan free volume and Flory-Huggins thermodynamic models. The first two models are completely predictive and based on the group contribution principle and activity coeffi-

Table 2

Ternary VLE data for the toluene (1)/methanol (2)/PVAC (3) system measured at 100 $^\circ\text{C}.$

<i>a</i> ₁	a2	$\phi_1 imes 100^{a}$	$\phi_2 imes 100$
0.145 ± 0.0018	0.075 ± 0.0029	0.02 ± 0.0906	0.28 ± 0.1642^{b}
0.168 ± 0.0021	0.100 ± 0.0040	0.90 ± 0.1168	0.41 ± 0.2598
0.196 ± 0.0024	0.116 ± 0.0046	1.61 ± 0.1264	1.08 ± 0.3010
0.236 ± 0.0029	0.138 ± 0.0055	1.80 ± 0.1268	1.30 ± 0.3274
0.255 ± 0.0032	0.148 ± 0.0058	2.07 ± 0.0975	1.71 ± 0.2573
0.300 ± 0.0037	0.184 ± 0.0073	2.73 ± 0.1376	1.67 ± 0.4064
0.315 ± 0.0039	0.196 ± 0.0077	3.39 ± 0.1283	2.24 ± 0.3847
0.336 ± 0.0042	0.222 ± 0.0087	4.03 ± 0.1303	2.22 ± 0.4181
0.387 ± 0.0048	0.237 ± 0.0094	4.75 ± 0.1734	3.31 ± 0.5326
0.379 ± 0.0047	0.242 ± 0.0095	4.97 ± 0.1296	3.49 ± 0.4068
0.416 ± 0.0052	0.269 ± 0.0106	5.17 ± 0.1355	3.40 ± 0.4447
0.435 ± 0.0054	0.288 ± 0.0114	5.92 ± 0.1438	3.79 ± 0.4777
0.484 ± 0.0060	0.307 ± 0.0121	6.21 ± 0.1623	4.31 ± 0.5315
0.487 ± 0.0061	0.333 ± 0.0131	7.27 ± 0.1667	4.30 ± 0.5686
0.514 ± 0.0064	0.348 ± 0.0137	7.03 ± 0.1537	4.35 ± 0.5333
0.610 ± 0.0076	0.395 ± 0.0156	7.79 ± 0.2309	4.58 ± 0.7934
0.573 ± 0.0071	0.390 ± 0.0154	9.10 ± 0.2031	5.54 ± 0.6816
0.586 ± 0.0073	0.407 ± 0.0161	8.66 ± 0.1757	5.21 ± 0.6147
0.682 ± 0.0085	0.469 ± 0.0185	10.80 ± 0.2593	6.02 ± 0.8780

^a Volume percent.

^b The uncertainties were calculated using Eqs. (A.1) through (A.13).

Table 3

Average absolute deviation, AD, between experimental and calculated activities.





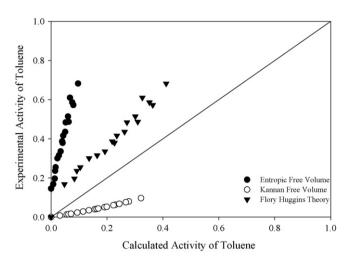


Fig. 11. The activity of toluene predicted by Entropic free volume, Kannan free volume and Flory-Huggins theory against the experimental measurements.

cients are calculated using group and group interaction parameters without any need for parameter regression from binary VLE data. Flory-Huggins theory is a molecular model and requires three interaction parameters, χ_{12} , χ_{13} , χ_{23} and molar volumes for the pure components as input parameters. The interaction parameter between two solvents, χ_{12} , were predicted from solubility parameters [20], while the interaction parameters between solvents and polymer (χ_{13} , χ_{23}) were regressed from binary VLE data by minimizing the following objective function (OBJ):

$$OBJ = \sum_{i=1}^{N_{DP}} \left(\ln a_i^{\text{calculated}} - \ln a_i^{\text{experimental}} \right)^2$$
(15)

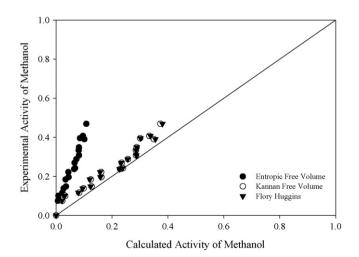


Fig. 12. The activity of methanol predicted by Entropic free volume, Kannan free volume and Flory-Huggins theory against the experimental measurements.

Regressed/calculated values and other input parameters used in Eqs. (13) and (14) are listed in Table 1. As shown in Fig. 10, the binary sorption data for both methanol and toluene have been correlated well with the Flory-Huggins theory using constant interaction parameters. In Figs. 11 and 12, the activities of solvents calculated by the Entropic free volume, Kannan free volume and Flory-Huggins theory have been plotted against the experimental data. The ternary VLE data and average absolute deviations, AD, between calculated and experimental activities are listed in Tables 2 and 3, respectively. Among the three thermodynamic models tested, the Flory-Huggins theory provides best results, on the other hand, its predictive ability is similar to that of the Kannan free volume model. The Kannan free volume term coupled to UNIFAC in the Kannan free volume model significantly improves its performance compared to Entropic free volume model. It is noted from Figs. 11 and 12 that each model provides better prediction for the activity of methanol.

7. Conclusion

In this study, binary and ternary VLE data for the toluene/PVAC, methanol/PVAC and toluene/methanol/PVAC systems have been measured by using a vapor-phase infrared spectroscopy. The accuracy of the experimental technique has been confirmed by good agreement between our binary data and literature data measured by other techniques. The IR technique not only allows to achieve higher pressure than that attainable in conventional gravimetric and volumetric sorption devices but also facilitates VLE data acquisition at a faster rate.

Ternary sorption results reveal that the presence of toluene does not influence the solubility of methanol, on the other hand, the solubility of toluene is lowered due to presence of methanol. Two fundamentally different types of thermodynamic models were used for the prediction of ternary VLE data. On the basis of average absolute deviation between experimental and calculated activities, Flory-Huggins theory provides the best results. The performance of the Kannan free volume model is better than that of Entropic free volume model. To our knowledge, this is the first study illustrating the use of the IR technique to measure VLE data in polymeric systems containing two solvents.

Appendix A

The uncertainties in the calculated activities and volume fractions of the solvents due to uncertainties in experimentally measured quantities ($\delta m_{\rm pd}$, $\delta V_{\rm T}$, $\delta V_{\rm Ti}$, δH_i , δm_i , δT) were evaluated by assuming that the measured quantities have a Gaussian distribution about their mean values. According to this assumption, the total error in the activity (δa_i) and volume fraction ($\delta \phi_i$) of solvent *i* can be obtained by combining the individual contributions in quadrature:

$$\delta a_{i} = \sqrt{\left(\frac{\partial a_{i}}{\partial H_{i}}\right)^{2} \delta H_{i}^{2} + \left(\frac{\partial a_{i}}{\partial m_{i}}\right)^{2} \delta m_{i}^{2} + \left(\frac{\partial a_{i}}{\partial T}\right)^{2} \delta T^{2}}$$
(A.1)

$$\delta\phi_{i} = \sqrt{A^{2}\delta m_{\rm pd}^{2} + B^{2}\delta V_{\rm T}^{2} + C^{2}\delta V_{\rm T1}^{2} + D^{2}\delta V_{\rm T2}^{2} + E^{2}\delta H_{1}^{2} + F^{2}\delta H_{2}^{2} + G^{2}\delta m_{1}^{2} + H^{2}\delta m_{2}^{2}}$$

where the partial derivatives appearing in Eqs. (A.1) and (A.2) are defined as follows:

$$\left(\frac{\partial a_i}{\partial H_i}\right) = \left(\frac{\partial a_i}{\partial P_i}\right) \left(\frac{\partial P_i}{\partial \rho_{gi}}\right) \left(\frac{\partial \rho_{gi}}{\partial H_i}\right)$$
(A.3)

$$\left(\frac{\partial a_i}{\partial m_i}\right) = \left(\frac{\partial a_i}{\partial P_i}\right) \left(\frac{\partial P_i}{\partial \rho_{gi}}\right) \left(\frac{\partial \rho_{gi}}{\partial m_i}\right)$$
(A.4)

$$\left(\frac{\partial a_i}{\partial T}\right) = \left(\frac{\partial a_i}{\partial P_i}\right) \left(\frac{\partial P_i}{\partial T}\right) \tag{A.5}$$

$$A = \left(\frac{\partial \phi_i}{\partial m_{\rm pd}}\right) = \left(\frac{\partial \phi_i}{\partial m_{\rm pd}}\right) + \sum_{j=1}^2 \left(\frac{\partial \phi_i}{\partial m_{\rm jp}}\right) \left(\frac{\partial m_{\rm jp}}{\partial V_{\rm g}}\right) \left(\frac{\partial V_{\rm g}}{\partial m_{\rm pd}}\right) \quad (A.6)$$

$$B = \left(\frac{\partial \phi_i}{\partial V_{\rm T}}\right) = \sum_{j=1}^2 \left(\frac{\partial \phi_i}{\partial m_{\rm jp}}\right) \left(\frac{\partial m_{\rm jp}}{\partial V_{\rm g}}\right) \left(\frac{\partial V_{\rm g}}{\partial V_{\rm T}}\right) \tag{A.7}$$

$$C = \left(\frac{\partial \phi_i}{\partial V_{T1}}\right) = \left(\frac{\partial \phi_i}{\partial m_{1p}}\right) \left(\frac{\partial m_{1p}}{\partial m_{T1}}\right) \left(\frac{\partial m_{T1}}{\partial V_{T1}}\right) + \sum_{j=1}^2 \left(\frac{\partial \phi_i}{\partial m_{jp}}\right) \left(\frac{\partial m_{jp}}{\partial V_g}\right) \left(\frac{\partial V_g}{\partial m_{T1}}\right) \left(\frac{\partial m_{T1}}{\partial V_{T1}}\right)$$
(A.8)

$$D = \left(\frac{\partial \phi_i}{\partial V_{T2}}\right) = \left(\frac{\partial \phi_i}{\partial m_{2p}}\right) \left(\frac{\partial m_{2p}}{\partial m_{T2}}\right) \left(\frac{\partial m_{T2}}{\partial V_{T2}}\right) + \sum_{j=1}^2 \left(\frac{\partial \phi_i}{\partial m_{jp}}\right) \left(\frac{\partial m_{jp}}{\partial V_g}\right) \left(\frac{\partial V_g}{\partial m_{T2}}\right) \left(\frac{\partial m_{T2}}{\partial V_{T2}}\right)$$
(A.9)

$$E = \left(\frac{\partial \phi_i}{\partial H_1}\right) = \left(\frac{\partial \phi_i}{\partial m_{1p}}\right) \left(\frac{\partial m_{1p}}{\partial \rho_{g1}}\right) \left(\frac{\partial \rho_{g1}}{\partial H_1}\right) + \sum_{j=1}^2 \left(\frac{\partial \phi_i}{\partial m_{jp}}\right) \left(\frac{\partial m_{jp}}{\partial V_g}\right) \left(\frac{\partial V_g}{\partial \rho_{g1}}\right) \left(\frac{\partial \rho_{g1}}{\partial H_1}\right)$$
(A.10)

$$F = \left(\frac{\partial \phi_i}{\partial H_2}\right) = \left(\frac{\partial \phi_i}{\partial m_{2p}}\right) \left(\frac{\partial m_{2p}}{\partial \rho_{g2}}\right) \left(\frac{\partial \rho_{g2}}{\partial H_2}\right) + \sum_{j=1}^2 \left(\frac{\partial \phi_i}{\partial m_{jp}}\right) \left(\frac{\partial m_{jp}}{\partial V_g}\right) \left(\frac{\partial V_g}{\partial \rho_{g2}}\right) \left(\frac{\partial \rho_{g2}}{\partial H_2}\right)$$
(A.11)

$$G = \left(\frac{\partial \phi_i}{\partial m_1}\right) = \left(\frac{\partial \phi_i}{\partial m_{1p}}\right) \left(\frac{\partial m_{1p}}{\partial \rho_{g1}}\right) \left(\frac{\partial \rho_{g1}}{\partial m_1}\right) + \sum_{j=1}^2 \left(\frac{\partial \phi_i}{\partial m_{jp}}\right) \left(\frac{\partial m_{jp}}{\partial V_g}\right) \left(\frac{\partial V_g}{\partial \rho_{g1}}\right) \left(\frac{\partial \rho_{g1}}{\partial m_1}\right)$$
(A.12)

$$F = \left(\frac{\partial \phi_i}{\partial m_2}\right) = \left(\frac{\partial \phi_i}{\partial m_{2p}}\right) \left(\frac{\partial m_{2p}}{\partial \rho_{g2}}\right) \left(\frac{\partial \rho_{g2}}{\partial m_2}\right) + \sum_{j=1}^2 \left(\frac{\partial \phi_i}{\partial m_{jp}}\right) \left(\frac{\partial m_{jp}}{\partial V_g}\right) \left(\frac{\partial V_g}{\partial \rho_{g2}}\right) \left(\frac{\partial \rho_{g2}}{\partial m_2}\right)$$
(A.13)

The derivatives required in Eqs. (A.3)-(A.13) were calculated using Eqs. (1)-(6).

(A.2)

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