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Can measurements of electric dipole moments determine the seesaw parameters?

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ABSTRACT: In the context of the supersymmetrized seesaw mechanism embedded in the Minimal Supersymmetric Standard Model (MSSM), complex neutrino Yukawa couplings can induce Electric Dipole Moments (EDMs) for the charged leptons, providing an additional route to seesaw parameters. However, the complex neutrino Yukawa matrix is not the only possible source of CP violation. Even in the framework of Constrained MSSM (CMSSM), there are additional sources, usually attributed to the phases of the trilinear soft supersymmetry breaking couplings and the mu-term, which contribute not only to the electron EDM but also to the EDMs of neutron and heavy nuclei. In this work, by combining bounds on various EDMs, we analyze how the sources of CP violation can be discriminated by the present and planned EDM experiments.

KEYWORDS: Neutrino Physics, CP violation, Supersymmetry Phenomenology.

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1. Introduction

The atmospheric and solar neutrino data [1] as well as the KamLAND [2] and K2K [3]results provide strong evidence for nonzero neutrino mass. On the other hand, from kinematical studies [4] and cosmological observations [5], the neutrinos are known to be much lighter than the other fermions. There are several models that generate tiny yet nonzero masses for neutrinos (see, e.q. [6]) among which the seesaw mechanism [7] is arguably the most popular one. This mechanism introduces three Standard Model (SM) singlet neutrinos with masses, M_N , which lie far above the electroweak scale. It has been shown that for $M_i > 10^9 \text{ GeV}$, decays of the right-handed neutrinos in the early Universe can explain the baryon asymmetry of the universe [8]. In addition to this, M_N lies at intermediate scales which are already marked by other phenomena including supersymmetry breaking scale, gauge coupling unification scale and the Peccei-Quinn scale. This rough convergence of scales of seemingly distinct phenomena might be related to their common or correlated origin dictated by first principles stemming, possibly, from superstrings. For probing physics at ultra high energies which are obviously beyond the reach of any man-made accelerator in foreseeable future, it is necessary to analyze and determine the effects of right-handed neutrinos on the low-energy observables.

The Minimal Supersymmetric Standard Model (MSSM), a direct supersymmetrization of the SM using a minimal number of extra fields, solves the gauge hierarchy problem; moreover, it provides a natural candidate for cold dark matter in the universe. For explaining the neutrino data within the seesaw scheme, the MSSM spectrum should be enlarged by right-handed neutrino supermultiplets. The resulting model, which we hereafter call MSSM-RN, is described by the superpotential

$$W = Y_{\ell}^{ij} \epsilon_{\alpha\beta} H_d^{\alpha} E_i L_j^{\beta} - Y_{\nu}^{ij} \epsilon_{\alpha\beta} H_u^{\alpha} N_i L_j^{\beta} + \frac{1}{2} M_{ij} N_i N_j - \mu \epsilon_{\alpha\beta} H_d^{\alpha} H_u^{\beta} , \qquad (1.1)$$

whose quark sector, not shown here, is the same as in the MSSM. Here α, β are SU(2) indices, i, j are generation indices, $L_{j\beta}$ consist of lepton doublets $(\nu_{jL}, \ell_{jL}^-)_{\beta}$, and E_i contain left-handed anti-leptons ℓ_{iL}^+ . The superfields N_i contain anti right-handed neutrinos. Without loss of generality, one can rotate and rephase the fields to make Yukawa couplings of charged leptons (Y_ℓ) as well as the mass matrix of the right-handed neutrinos (M_{ij}) real diagonal. In the calculations below, we will use this basis.

In general, the soft supersymmetry-breaking terms (the mass-squared matrices and trilinear couplings of the sfermions) can possess flavor-changing entries which facilitate a number of flavor-changing neutral current processes in the hadron and lepton sectors. The existing experimental data thus put stringent bounds on flavor-changing entries of the soft terms. For instance, flavor-changing entries of the soft terms in the lepton sector can result in sizeable $\mu \to e\gamma$, $\tau \to e\gamma$ and $\tau \to \mu\gamma$. This motivates us to go to the mSUGRA [9] or constrained MSSM framework where soft terms of a given type unify at the scale of gauge coupling unification. In other words, at the GUT scale, we take

$$\mathcal{L}_{soft} = -m_0^2 (\tilde{L}_i^{\dagger} \tilde{L}_i + \tilde{E}_i^{\dagger} \tilde{E}_i + \tilde{N}_i^{\dagger} \tilde{N}_i + H_d^{\dagger} H_d + H_u^{\dagger} H_u) - \frac{1}{2} m_{1/2} (\tilde{B}\tilde{B} + \tilde{W}\tilde{W} + \tilde{g}\tilde{g} + \text{H.c.}) - \left(\frac{1}{2} \epsilon_{\alpha\beta} b_H \mu H_d^{\alpha} H_u^{\beta} + \text{H.c.}\right) - (A_\ell^{ij} \epsilon_{\alpha\beta} H_d^{\alpha} \tilde{E}_i \tilde{L}_j^{\beta} - A_\nu^{ij} \epsilon_{\alpha\beta} H_u^{\alpha} \tilde{N}_i \tilde{L}_j^{\beta} + \text{H.c.}) - \left(\frac{1}{2} B_\nu M_i \tilde{N}^i \tilde{N}^i + \text{H.c.}\right).$$

$$(1.2)$$

Here $A_{\ell} = a_0 Y_{\ell}$ and $A_{\nu} = a_0 Y_{\nu}$. The last term is the lepton number violating neutrino bilinear soft term which is called the neutrino *B*-term.

As first has been shown in [10], at lower scales, the Lepton Flavor Violating (LFV) Yukawa coupling Y_{ν} will induce LFV contributions to the soft masses of the left-handed sleptons. Consequently, the strong bounds on LFV rare decays can be translated into bounds on the seesaw parameters. In section 4, we will discuss these bounds in detail. If we assume that the soft terms are of the form $(1.2)^1$ and Y_{ν} is the only source of LFV then mass-squares of left-handed sleptons can be considered as another source of information on the seesaw parameters. It is shown in ref. [11] that, by knowing all the entries of the mass matrices of neutrinos and left-handed sleptons (both their norms and phases), we can extract all the seesaw parameters. However, such a possibility at the moment does not seem to be achievable. As a result, one has to resort to finding new sources of information on the seesaw parameters.

In general, the neutrino Yukawa coupling, Y_{ν} , can possess CP-odd phases, and thus induces electric dipole moments (EDM) for charged leptons [12, 13]. It has already been suggested to extract seesaw parameters from the electron EDM, d_e [14]. However, for deriving any information from d_e we must be aware of other sources of CP violation that can give a significant contribution to d_e . In the model we are using, there are three extra sources of CP violation in the leptonic sector: the physical phases of the μ parameter,

¹In practice, confirmation of this assumption is not possible. However, this assumption will be refuted if we find that the flavor mixing in the right-handed sector is comparable to that in the left-handed sector.

the universal trilinear coupling a_0 and the neutrino *B*-term.² As first has been shown in [16], the phase of the neutrino *B*-term can induce a contribution to d_e . In this paper, for simplicity, we will set $B_{\nu} = 0$. The phases of a_0 and μ can result in comparable electric dipole moments for the electron, neutron and mercury. More precisely, they induce $d_e \sim$ $(m_e/m_d)d_d \sim (m_e/m_u)d_u \sim e(m_e/m_d)\tilde{d}_d \sim e(m_e/m_u)\tilde{d}_u$, where \tilde{d}_u and \tilde{d}_d respectively are the chromo electric dipole moments (CEDM) of up and down quarks which contribute to the EDMs of mercury (d_{Hg}) and deuteron (d_D) . In principle, the phases of a_0 and μ can induce d_D which may be detectable in future searches [17]. On the other hand, as shown in the appendix, the quark EDMs and CEDMs induced by the phases of Y_{ν} are too small to be detectable in near future. Therefore, if complex Y_{ν} is the only source of CP violation, we expect d_D to be too small to be detectable in the near future $(d_D$ is measured with ionized deuteron which is depleted from electrons). Based on these observations we raise the following question: Considering the limited accuracy of the experiments, is it possible to discern the source of the CP violation? The present paper addresses this very question.

This paper is organized as follows. In section 2, we show that there is a "novel" contribution to d_{ℓ} which is proportional to $m_{1/2}$, and it results from the renormalization group running of the trilinear couplings. As will be demonstrated in the text, the new contribution can dominate over those previously discussed in the literature. In section 3, we first review the experimental bounds on the EDMs. We then review how observable EDMs of neutron and different nuclei are related to the EDMs and CEDMs of the quarks. In section 4, we represent our numerical results and analyze the prospects of identifying the source of CP violation. Conclusions are given in section 5.

2. Contribution of Y_{ν} to EDMs

In this section, we review the effects of complex Y_{ν} on the charged lepton EDMs which has been previously calculated in the literature. We also discuss a new effect which has been so far overlooked. In the end, we point out an unexpected suppression that occurs when we insert realistic values for the mSUGRA parameters. Throughout this section we will assume that complex Y_{ν} is the only source of CP-violation.

As it is shown in [13], inserting LFV radiative corrections to A_{ℓ} and $m_{\tilde{L}}^2$ in the diagram shown in figure 1, we obtain a contribution to the EDM of the corresponding charged lepton. By inserting one-loop lepton flavor violating corrections to A_{ℓ} and $m_{\tilde{L}}^2$, we obtain

$$\vec{d_i}^{(1)} = (-e)\eta_{d_e} m_{\ell i} \frac{2\alpha}{(4\pi)^5} \sum_a \sum_{k,j,m} \left(\frac{V_{1a}}{c_w}\right) \left(\frac{V_{1a}}{c_w} + \frac{V_{2a}}{s_w}\right) \frac{a_0 m_a}{|m_a|^6} g\left(\frac{m_{\tilde{L}}^2}{m_a^2}, \frac{m_{\tilde{E}}^2}{m_a^2}\right) \times \\ \times \operatorname{Im}\left[(Y_{\nu}^{ki})^* Y_{\nu}^{kj} \left(Y_{\nu}^{mj}\right)^* Y_{\nu}^{mi} \right] \cdot \left(-2m_0^2 \operatorname{Log} \frac{M_{GUT}^2}{M_k^2}\right) \vec{S} , \qquad (2.1)$$

²In fact, apart from the phases of a_0 and μ there are two more sources of CP-violation: the phase of the CKM matrix and the QCD theta term. The contribution of the former to EDMs of charged leptons is negligible [15]. For the latter we assume that there is a mechanism like the Peccei-Quinn mechanism that suppresses the CP-odd topological term in the QCD lagrangian.

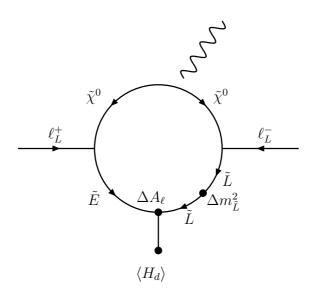


Figure 1: A contribution to the charged lepton dipole moments.

where \vec{S} is the spin of the lepton, V is the mixing matrix of the neutralinos, m_a are the masses of the neutralinos and

$$g(x_L, x_E) = \frac{1}{2(x_E - x_L)^2} \left(\frac{1 - x_L^2 + 2x_L \log x_L}{(1 - x_L)^3} - \frac{1 - x_E^2 + 2x_E \log x_E}{(1 - x_E)^3} \right) + \frac{1}{2(x_E - x_L)} \left(\frac{5 - 4x_L - x_L^2 + 2(1 + 2x_L) \log x_L}{(1 - x_L)^4} \right).$$
(2.2)

The main contribution to the diagram shown in figure 1 comes from the momenta around the supersymmetry breaking scale $(M_{\rm susy})$; as a result we have to insert the values of ΔA_{ℓ} and $\Delta m_{\tilde{L}}^2$ at $M_{\rm susy}$ by taking into account the effects of running of the effective operators from the scale that the right-handed neutrinos decouple down to $M_{\rm susy}$. It can be shown that the LFV corrections to the slepton masses remain unchanged between the two scales. However, lowering energy from the right-handed neutrino scale down to $M_{\rm susy}$, ΔA_{ℓ} changes significantly. Here, the main effect comes from the gauge interaction and we can practically neglect the effects of Y_{ℓ} on the running. The factor $\eta_{d_e} \simeq 1.5$ in eq. (2.1) takes care of the running of ΔA_{ℓ} .

Now, let us discuss the running of the relevant parameters from the GUT scale down to the right-handed neutrino scale. Let us take $M_{GUT} = 2 \times 10^{16} \text{ GeV}$ and $M_N \sim Y_{\nu}^2 \langle H_u \rangle^2 / m_{\nu}$. For $Y_{\nu} \sim 1$ and $m_{\nu} \sim 0.1 \text{ eV}$, we find $M_N \sim 10^{14} \text{ GeV}$ so we expect that the running of parameters from the GUT scale down to the right-handed neutrino mass scale to be suppressed by $\text{Log}(M_N^2/M_{GUT}^2)/(16\pi^2) \sim 0.1$. Thus, we can practically neglect the running of the gauge and Yukawa couplings as well as the gaugino and right-handed neutrino masses in this range. But there is a subtlety to be noted here. Although the dominant terms of both ΔA_{ℓ} and $\Delta m_{\tilde{L}}^2$ are enhanced by a large log factor $\text{Log} \frac{M_{GUT}^2}{M_k^2}$, the effect in eq. (2.1), which is given by $\text{Im}(\Delta A_{\ell} \Delta m_{\tilde{L}}^2)$, contains only one factor of $\text{Log} \frac{M_{GUT}^2}{M_k^2}$. This is because the leading-log parts of ΔA_{ℓ} and $\Delta m_{\tilde{L}}^2$ have the same flavor structure $\sum_k (Y_{\nu}^{ki})^* \operatorname{Log}(M_{GUT}^2/M_k^2) Y_{\nu}^{kj}$, and thus, $\operatorname{Im}\left[(\Delta A_{\ell})_{leading-log}(\Delta m_{\tilde{L}}^2)_{leading-log}\right] = 0$ and the dominant contribution to $\operatorname{Im}[\Delta A_{\ell} \Delta m_{\tilde{L}}^2]$ comes from $\operatorname{Im}\left[(\Delta A_{\ell})_{leading-log}(\Delta m_{\tilde{L}}^2)_{finite}\right]$ and $\operatorname{Im}\left[(\Delta A_{\ell})_{finite}(\Delta m_{\tilde{L}}^2)_{leading-log}\right]$ which contain only one large log factor. If there is a two-loop contribution to the A_{ℓ} term or mass matrix of the left-handed sleptons $[(\Delta A_{\ell})_{2-loop} \text{ or } (\Delta m_{\tilde{L}}^2)_{2-loop}]$ with two large-log factors, $\operatorname{Im}[\Delta A_{\ell}^{2-loop}(\Delta m_{\tilde{L}}^2)_{L-L}^{1-loop})]$ and $\operatorname{Im}\left[(\Delta A_{\ell})_{L-L}^{1-loop}(\Delta m_{\tilde{L}}^2)_{2-loop}^{2-loop})\right]$ (here L-L indices denote leading-log contributions) can be comparable to $\operatorname{Im}\left[(\Delta A_{\ell})_{L-L}^{1-loop}(\Delta m_{\tilde{L}}^2)_{l-L}^{1-loop}]$. Consequently, inserting the 2-loop correction to A_{ℓ} and 1-loop correction to $\Delta m_{\tilde{L}}^2$ (or vice-versa) in the diagram shown in figure 1, we get an effect comparable to (or dominant over) eq. (2.1). The diagrams shown in figures 2 and 3 give the dominant two-loop corrections to (ΔA_{ℓ}) and $(\Delta m_{\tilde{L}}^2)$, respectively. The leading-log parts of the diagrams are^3

$$(\Delta A_{\ell})_{ik} = \frac{3}{2} m_{1/2} \frac{g^2}{(4\pi)^4} \sum_j Y_{\ell}^i (Y_{\nu}^{ji})^* Y_{\nu}^{jk} \left(\text{Log} \frac{M_{GUT}^2}{M_j^2} \right)^2$$
(2.3)

and

$$(\Delta m_{\tilde{L}}^2)_{ik} = 3m_{1/2}a_0 \frac{g^2}{(4\pi)^4} \sum_j (Y_{\nu}^{ji})^* Y_{\nu}^{jk} \left(\text{Log} \frac{M_{GUT}^2}{M_j^2} \right)^2.$$
(2.4)

Inserting these diagrams in the diagram shown in figure 1 we arrive at the following result

$$\begin{split} \vec{d_i}^{(2)} &= (-e)\eta_{d_e} m_{\ell i} \frac{-2\alpha}{(4\pi)^7} \frac{3g^2}{2} \sum_a \sum_{k,j,m} \left(\frac{V_{1a}}{c_w}\right) \left(\frac{V_{1a}}{c_w} + \frac{V_{2a}}{s_w}\right) \frac{m_{1/2} m_a}{|m_a|^6} g\left(\frac{m_{\tilde{L}}^2}{m_a^2}, \frac{m_{\tilde{E}}^2}{m_a^2}\right) \times \\ & \times \operatorname{Im}[(Y_{\nu}^{ki})^* Y_{\nu}^{kj} (Y_{\nu}^{mj})^* Y_{\nu}^{mi}] \cdot (3m_0^2 - a_0^2) \left(\operatorname{Log} \frac{M_{GUT}^2}{M_k^2}\right)^2 \operatorname{Log} \frac{M_{GUT}^2}{M_m^2} \vec{S} \,. \end{split}$$

This effect had been overlooked in the literature.

Finally, as discussed in [13], in large $\tan \beta$ domain the dominant contribution takes the following form:

$$\vec{d_i}^{(3)} = e \frac{8\alpha}{(4\pi)^7} \times \\ \times \sum_a \left(\frac{V_{1a}}{c_w}\right) \left(\frac{V_{1a}}{c_w} + \frac{V_{2a}}{s_w}\right) \frac{\mu m_{\ell i} m_a}{|m_a|^8 v^2} \frac{\tan\beta}{\cos^2\beta} (9m_0^4 + 9a_0^2 m_0^2 + 2a_0^4) h\left(\frac{m_{\tilde{L}}^2}{m_a^2}, \frac{m_{\tilde{E}}^2}{m_a^2}\right) \times \\ \times \sum_{kjm} \operatorname{Im}[(Y_{\nu}^{ki})^* Y_{\nu}^{kj} m_{\ell j}^2 (Y_{\nu}^{mj})^* Y_{\nu}^{mi}] \left(\operatorname{Log} \frac{M_{GUT}^2}{M_k^2}\right)^2 \operatorname{Log} \frac{M_{GUT}^2}{M_m^2} \vec{S},$$
(2.5)

where

$$h(x_L, x_E) = -\frac{1}{(x_E - x_L)^3} \left(\frac{1 - x_L^2 + 2x_L \log x_L}{(1 - x_L)^3} - \frac{1 - x_E^2 + 2x_E \log x_E}{(1 - x_E)^3} \right) - \frac{1 - x_E^2 + 2x_E \log x_E}{(1 - x_E)^3} = -\frac{1 - x_E^2 + 2x_E \log x_E}{(1 -$$

³Note that there are similar diagrams with \tilde{B} replacing \tilde{W} in the loops. The effects of the latter is less than 20% of the ones we are considering here. Such a precision is beyond the scope of this paper.

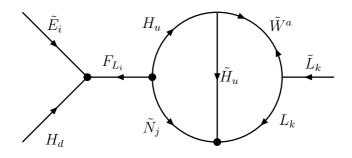


Figure 2: The two-loop correction to A_{ℓ} given by $m_{1/2}$. Vertices marked with circles are Yukawa vertices and the rest are gauge vertices. F_{L_i} is the auxiliary field associated with L_i .

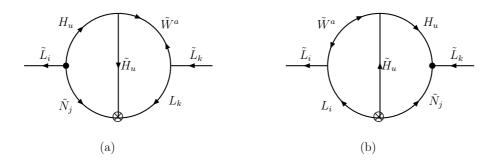


Figure 3: The two-loop corrections to $m_{\tilde{L}}$ given by $m_{1/2}$. Vertices marked with \otimes and circles are Yukawa vertices and A-terms, respectively. The rest are gauge vertices.

$$-\frac{1}{2(x_E - x_L)^2} \left(\frac{5 - 4x_L - x_L^2 + 2(1 + 2x_L) \text{Log} x_L}{(1 - x_L)^4} + \frac{5 - 4x_E - x_E^2 + 2(1 + 2x_E) \text{Log} x_E}{(1 - x_E)^4} \right).$$
(2.6)

Note that one should insert the value of μ at the supersymmetry breaking scale in eq. (2.5).

To evaluate the order of magnitude of the EDMs, at first sight it seems that we can simply set all the supersymmetric parameters to some common scale m_{susy} and take the values of the functions f and h in eqs. (2.1), (2.5), (2.5) to be numbers of order 1. However, this is not a valid simplification because the functions f and h rapidly decrease when their arguments fall below unity. In the mSUGRA model we expect the mass of the lightest neutralino to be smaller than that of sfermions. As a result, we expect h and g to be smaller than one. In section 4, we will see that this effect gives rise to a suppression by two to three orders of magnitude.

3. Effects of the phases of μ and a_0 on EDMs

In this section, we first review the current bounds on d_e , d_{μ} , d_D , d_{Hg} and d_n and the prospects of improving them. We then review how we can write them in terms of $Im(\mu)$ and $Im(a_0)$.

Electron EDM d_e : The present bound on the EDM of electron is

$$d_e < 1.7 \times 10^{-27} \ e \ cm$$
 at 95 % CL [18] (3.1)

DeMille and his Yale group are running an experiment that uses the PbO molecules to probe d_e . Within three years they can reach a sensitivity of 10^{-29} e cm [19] and hopefully down to a sensitivity of 10^{-31} e cm within five years. There are proposals [20] for probing d_e down to 10^{-35} e cm level. In sum there is a very good prospect of measuring d_e in future [21].

Neutron EDM d_n : The present bound on d_n [22] is

$$d_n < 6.3 \times 10^{-26} e \text{ cm}$$
 at 90 % CL (3.2)

This bound will be improved considerably by LANSCE [23] which will be able to probe d_n down to 4×10^{-28} e cm.

Muon EDM, d_{μ} : The present bound on d_{μ} [18] is

$$d_{\mu} < 7 \times 10^{-19} e \text{ cm} \,. \tag{3.3}$$

There are proposals to measure d_{μ} down to 10^{-24} e cm [24]. Using the storage ring of a neutrino factory, measurement of d_{μ} down to 5×10^{-26} will become a possibility [25].

Mercury EDM d_{Hg} : The present bound on d_{Hg} is

$$|d_{Hq}| < 2.1 \times 10^{-28} e \text{ cm}.$$
(3.4)

which can be improved by a factor of four [26].

Deuteron EDM d_D : The present bound on d_D is very weak; however, there are proposals [17] to probe d_D down to

$$|d_D| < (1-3) \times 10^{-27} \ e \ \text{cm} \,. \tag{3.5}$$

Different sources of CP-violation affect the EDMs listed above differently. As a result, in principle by combining the information on these observables, we can discriminate between different sources of CP-violation. However to perform such an analysis we must be able to express the EDMs in terms of $\text{Im}[a_0]$, $\text{Im}[\mu]$ and $\text{Im}[Y_{\nu}]$. In the previous section, we reviewed the effects of complex Y_{ν} on d_e . The effects of complex a_0 and μ on d_e are also well understood. However, writing d_n , d_{Hg} and d_D in terms of the sources of CP-violation is more complicated. To do so, we first have to express d_n , d_{Hg} and d_D in terms of the EDMs and CEDMs of light quarks (namely, d_u , d_d , d_s , \tilde{d}_u , \tilde{d}_d and \tilde{d}_s) and then calculate the quark EDMs and CEDMs in terms of $\text{Im}[a_0]$, $\text{Im}[\mu]$ and $\text{Im}[Y_{\nu}]$. The quark EDMs and CEDMs in terms of $\text{Im}[a_0]$ and $\text{Im}[\mu]$ have already been calculated in the literature. In this paper we have used the results of ref. [27]. As we discussed in the appendix, the effects of $\text{Im}[Y_{\nu}]$ on the quark EDMs and CEDMs are negligible. Unfortunately, the first step (expressing d_n , d_{Hg} and d_D in terms of the quark EDMs and CEDMs) is quite challenging. Let us consider them one by one.

- $d_n(d_q, \tilde{d}_q)$: Despite of the rich literature on d_n in terms of the quark EDMs and CEDMs, the results are quite model dependent. For example, the SU(3) chiral model [28] and QCD sum rules [29] predict different contributions from \tilde{d}_u and \tilde{d}_d to d_n . Considering these discrepancies in the literature, in this paper we do not use bounds on d_n in our analysis. As it is shown in [30], information on d_n can help to refute the "cancelation" scenario. We will come back to this point later.
- $d_{Hg}(d_q, \tilde{d}_q)$: There is an extensive literature on d_{Hg} [31]. In this paper, following ref. [32], we will interpret the bound on d_{Hg} as

$$|\tilde{d}_d - \tilde{d}_u| < 2 \times 10^{-26} \text{ cm.}$$
 (3.6)

As shown in the recent paper [33], the EDM of electrons in the mercury atom can give a non-negligible contribution to d_{Hg} . As a result, improvements on the bound on d_{Hg} will not be very helpful for us to discriminate between different sources of CP-violation; *i. e.*, d_{Hg} also obtains a correction from complex Y_{ν} through d_e .

 $d_D(d_q, d_q)$: Searches for d_D can serve as an ideal probe for the existence of sources of CPviolation other than complex Y_{ν} because *i*) there is a good prospect of improving the bound on d_D [17]; *ii*) an ionized deuteron does not contain any electrons and hence we expect only a negligible and undetectable contribution from Y_{ν} to d_D .

To calculate d_D in terms of quark EDMs and CEDMs, two techniques have been suggested in the literature: *i*) QCD sum rules [34] and *ii*) SU(3) chiral theory [35]. Within the error bars, the two models agree on the contribution from $\tilde{d}_d - \tilde{d}_u$ which is the dominant one. However, the results of the two models on the sub-dominant contributions are not compatible. Apart from this discrepancy, there is a large uncertainty in the contribution of the dominant term:

$$d_D(d_q, \tilde{d}_q) \simeq -e(\tilde{d}_u - \tilde{d}_d) \, 5^{+11}_{-3} \,.$$
(3.7)

In this paper we take "the best fit" for our analysis.

4. Numerical analysis

In this section, we first describe how we produce the random seesaw parameters compatible with the data. We then describe the figures 4–9 and, in the end, discuss what can be inferred from the future data considering different possible situations one by one.

In figures 4–9, the dots marked with "+" represent d_e resulting from complex Y_{ν} . To extract random Y_{ν} and M_N compatible with data, we have followed the recipe described in [36] and solved the following two equations

$$\eta_{m_{\nu}}Y_{\nu}^{T}\frac{1}{M}Y_{\nu}(v^{2}\sin^{2}\beta)/2 = U \cdot \Phi \cdot M_{\nu}^{Diag} \cdot \Phi \cdot U^{T}$$

$$(4.1)$$

and

$$h \equiv Y_{\nu}^{\dagger} \text{Log} \frac{M_{GUT}}{M} Y_{\nu} = \begin{bmatrix} a & 0 & d \\ 0 & b & 0 \\ d^* & 0 & c \end{bmatrix},$$
(4.2)

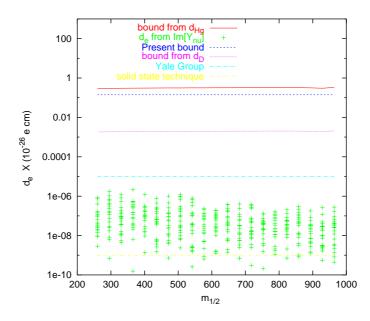


Figure 4: Electric dipole moment of the electron for $a_0 = 0$, $\tan \beta = 10$ and $\operatorname{sgn}(\mu) = +$. To draw the red solid and purple dotted lines, we have assumed that $\operatorname{Im}[\mu]$ is the only source of CP-violation and have taken $\tilde{d}_d - \tilde{d}_u$ equal to 2×10^{-26} cm and 2×10^{-28} cm, respectively to derive $\operatorname{Im}[\mu]$. To produce the dots, we have assumed that complex Y_{ν} is the only source of CP-violation and have randomly produced Y_{ν} compatible with the data. The blue dashed line is the present bound on d_e [18] and dot-dashed lines show the values of d_e that can be probed in the future [19, 20].

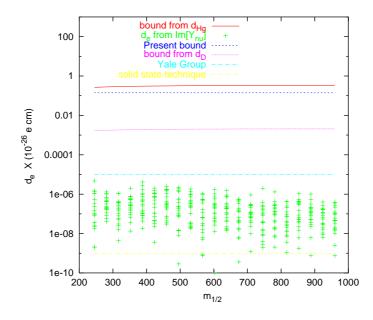


Figure 5: The same as figure 4 for $a_0 = 0$, $\tan \beta = 20$ and $\operatorname{sgn}(\mu) = +$.

where v = 247 GeV, M is the mass matrix of the right-handed neutrinos, U is the mixing matrix of neutrinos with $s_{13} = 0$ and Φ is $diag[1, e^{i\phi_1}, e^{i\phi_2}]$ with random values of ϕ_1 and ϕ_2 in the range $(0, 2\pi)$. Finally, $M_{\nu}^{Diag} = diag[m_1, \sqrt{m_1^2 + \Delta m_{21}^2}, \sqrt{m_1^2 + \Delta m_{31}^2}]$ where

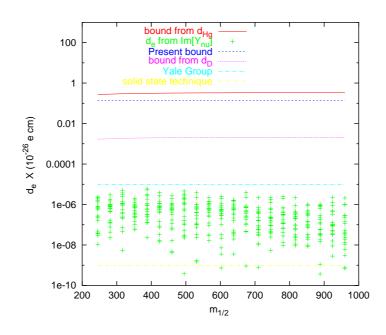


Figure 6: The same as figure 4 for $a_0 = 0$, $\tan \beta = 20$ and $\operatorname{sgn}(\mu) = -$.

 m_1 picks up random values between 0 and 0.5 eV in a linear scale. The upper limit on m_1 is what has been found in [37] by taking the dark energy equation of state a free (but constant) parameter. In the above equation, $\eta_{m_{\nu}}$ takes care of the running of the neutrino mass matrix from M to M_{susy} . Since the deviation of $\eta_{m_{\nu}}$ from unity is small [38], we have set $\eta_{m_{\nu}} = 1$.

In order to satisfy the strong bounds on $\operatorname{Br}(\mu \to e\gamma)$ [18] and $\operatorname{Br}(\tau \to \mu\gamma)$ [41], the matrix h, defined in eq. (4.2), is taken to have this specific pattern with zero $e\mu$ and $\mu\tau$ elements. Actually these branching ratios put bounds on $(\Delta m_{\tilde{L}}^2)_{e\mu}$ and $(\Delta m_{\tilde{L}}^2)_{\mu\tau}$ rather than on $h_{e\mu}$ and $h_{\mu\tau}$. Notice that only the dominant term of $\Delta m_{\tilde{L}}^2$ is proportional to h. There is also a subdominant "finite" contribution to $\Delta m_{\tilde{L}}^2$ which is about 10% of the dominant effect and is not proportional to the matrix h [13]. As we saw in section 2, this finite part plays a crucial role in giving rise to EDMs because the dominant leading-log part cancels out. Nonetheless, for extracting the seesaw parameters, 20% accuracy is enough and we can neglect the subdominant part and take $\Delta m_{\tilde{L}}^2$ proportional to the matrix h. In eq. (4.2), a, b, c are real numbers which take random values between 0 and 5. On the other hand, |d| takes random values between 0 and the upper bound from $\operatorname{Br}(\tau \to e\gamma)$ [42]. To calculate the upper bound on |d|, we have used the formulae derived in ref. [43]. The phase of d takes random values between 0 and 2π . With the above bounds on the random variables, the Yukawa couplings can be relatively large, giving rise to

$$\operatorname{Im}\left[Y_{\nu}^{\dagger}\operatorname{Log}^{2}\frac{M_{GUT}^{2}}{M_{N}^{2}}Y_{\nu}Y_{\nu}^{\dagger}\operatorname{Log}\frac{M_{GUT}^{2}}{M_{N}^{2}}Y_{\nu}\right]_{ee} \sim \operatorname{few} \times 10$$

$$(4.3)$$

and

$$\operatorname{Im}\left[Y_{\nu}^{\dagger}\operatorname{Log}\frac{M_{GUT}^{2}}{M_{N}^{2}}Y_{\nu}Y_{\nu}^{\dagger}Y_{\nu}\right]_{ee} \sim \operatorname{few} \times 0.1.$$

$$(4.4)$$

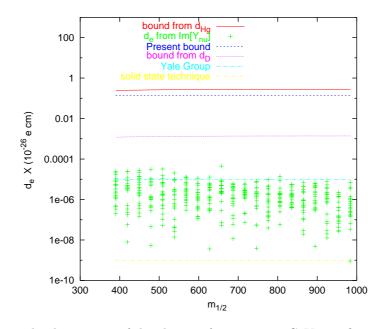


Figure 7: Electric dipole moment of the electron for $a_0 = 1000 \text{ GeV}$, $\tan \beta = 10$ and $\operatorname{sgn}(\mu) = +$. To draw the red solid and purple dotted lines, we have assumed that $\operatorname{Im}[a_0]$ is the only source of CP-violation and have taken $\tilde{d}_d - \tilde{d}_u$ equal to 2×10^{-26} cm and 2×10^{-28} cm, respectively to derive $\operatorname{Im}[a_0]$. To produce the dots, we have assumed that complex Y_{ν} is the only source of CP-violation and have randomly produced Y_{ν} compatible with the data. The blue dashed line is the present bound on d_e [18] and dot-dashed lines show the values of d_e that can be probed in the future [19, 20]

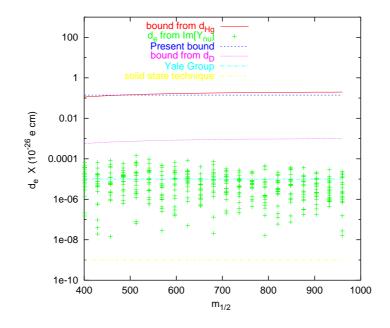


Figure 8: The same as figure 7 for $a_0 = 1000 \text{ GeV}$, $\tan \beta = 20 \text{ and } \operatorname{sgn}(\mu) = +$.

As we discussed in the end of section 2, because of the presence of the rapidly changing functions $g(x_L, x_R)$ and $h(x_L, x_R)$ in eqs. (2.1), (2.5), (2.5), the value of d_e strongly

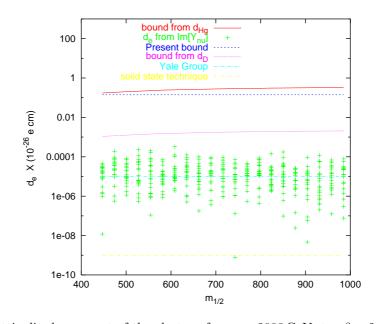


Figure 9: Electric dipole moment of the electron for $a_0 = 2000 \text{ GeV}$, $\tan \beta = 20$ and $\operatorname{sgn}(\mu) = +$. To draw the red solid and purple dotted lines, we have assumed that $\operatorname{Im}[\mu]$ is the only source of CP-violation and have taken $\tilde{d}_d - \tilde{d}_u$ equal to 2×10^{-26} cm and 2×10^{-28} cm, respectively to derive $\operatorname{Im}[\mu]$. To produce the dots, we have assumed that complex Y_{ν} is the only source of CP-violation and have randomly produced Y_{ν} compatible with the data. The blue dashed line is the present bound on d_e [18] and dot-dashed lines show the values of d_e that can be probed in the future [19, 20]

depends on the values of the supersymmetric parameters. To perform this analysis we have taken various values of $\tan \beta$ and a_0 and calculated the spectrum of the supersymmetric parameters along the $m_{1/2} - m_0$ strips parameterized in ref. [44]. Notice that ref. [44] has already removed the parameter range for which color or charge condensation takes place.

In the figures, we have also drawn the present bound on d_e [18] as well as the limits which can be probed in the future. The present bound is shown by a dashed dark blue line and lies several orders of magnitude above the d_e from phases of Y_{ν} . After five years of data-taking, the Yale group can probe d_e down to $10^{-31} \ e \ cm$ [19] which is shown with a dot-dashed cyan line in the figures. As it is demonstrated in the figures, only for large values of a_0 the effect of complex Y_{ν} on d_e can be probed by the Yale group and for most of the parameter space the effect remains beyond the reach of this experiment.

There are proposals [20] to use solid state techniques to probe d_e down to $10^{-35} e$ cm (shown with dot-dashed yellow line in the figure). In this case, as it can be deduced from the figure, we will have a great chance of being sensitive to the effects of the phases of Y_{ν} on d_e . However, unfortunately, the feasibility and time scale of the solid state technique is still uncertain.

Although for intermediate values of $\tan \beta$, the effect of the phases of Y_{ν} on d_e is very low (< 10⁻³⁰ e cm), its effect can still be much higher than the four-loop effect on d_e in the SM (the effect of the CP-violating phase of the CKM matrix) which is estimated to be ~ 10⁻³⁸ e cm [15]. In figures 4–6 as well as in figure 9, d_e resulting from $\text{Im}[\mu]$ is also depicted. The red solid lines in these figures show d_e from $\text{Im}[\mu]$ assuming that the corresponding d_{Hg} saturates the present bound [26]. As it is well-known, there are uncertainties both in the value of m_d [18] and in the interpretation of d_{Hg} in terms of more fundamental parameters \tilde{d}_u , \tilde{d}_d and \tilde{d}_s . To draw this curve we have assumed $m_d = 5 \text{ MeV}$ and $\tilde{d}_u - \tilde{d}_d < 2 \times 10^{-26}$ e cm. As it is shown in the figure this bound is weaker than even the present direct bound on d_e . The purple dotted lines in figures 4, 5, 6, 9, represent d_e induced by values of $\text{Im}[\mu]$ that give rise to $\tilde{d}_u - \tilde{d}_d = 2 \times 10^{-28} \text{ cm}$ (corresponding to $d_D = 10^{-27} e \text{ cm}$ and $d_D = 5e(\tilde{d}_d - \tilde{d}_u)$). Notice that these curves lie well below the direct bound on d_e but the Yale group will be able to probe even smaller values of d_e . Similarly in figures 7, 8, d_e resulting from $\text{Im}[a_0]$ is depicted.

The following comments are in order:

1) The combination of the seesaw parameters that enter the formula for d_e resulting from $\text{Im}[\Delta m_{\tilde{E}}^2 m_{\ell}^2 \Delta m_{\tilde{I}}^2]$ [see eq. (2.5)] is

$$\begin{split} \mathrm{Im} \left[Y_{\nu}^{\dagger} \mathrm{Ln}^2 \frac{M_{GUT}^2}{M^2} Y_{\nu} m_{\ell}^2 Y_{\nu}^{\dagger} \mathrm{Ln} \frac{M_{GUT}^2}{M^2} Y_{\nu} \right]_{ee} \simeq \\ \simeq m_{\tau}^2 \mathrm{Im} \left[\left(Y_{\nu}^{\dagger} \mathrm{Ln}^2 \frac{M_{GUT}^2}{M^2} Y_{\nu} \right)_{e\tau} \left(Y_{\nu}^{\dagger} \mathrm{Ln} \frac{M_{GUT}^2}{M^2} Y_{\nu} \right)_{\tau e} \right] \end{split}$$

where M is the mass matrix of the right-handed neutrinos. In contrast to this, the "new" effect given in eq. (2.5) is proportional to

$$\mathrm{Im}\left[Y_{\nu}^{\dagger}\mathrm{Ln}^{2}\frac{M_{GUT}^{2}}{M_{N}^{2}}Y_{\nu}Y_{\nu}^{\dagger}\mathrm{Ln}\frac{M_{GUT}^{2}}{M_{N}^{2}}Y_{\nu}\right]_{ee}$$

For the specific pattern of the h matrix shown in eq. (4.2) (with zero $e\mu$ element) this effect is also given by

$$\operatorname{Im}\left[\left(Y_{\nu}^{\dagger}\operatorname{Ln}^{2}\frac{M_{GUT}^{2}}{M_{N}^{2}}Y_{\nu}\right)_{e\tau}\left(Y_{\nu}^{\dagger}\operatorname{Ln}\frac{M_{GUT}^{2}}{M_{N}^{2}}Y_{\nu}\right)_{\tau e}\right].$$
(4.5)

In other words, the two effects are proportional to each other.

For the values of supersymmetric parameters chosen in figure 4 (that is, $sgn(\mu)=+$, $tan \beta = 10, a_0 = 0$), the "new" effect is dominant and is -5 times the effect previously discussed in the literature. However, for $a_0 = 1000$ GeV and 2000 GeV (figures 7, 8 and 9) the dominant contribution is the one given by eq. (2.5).

2) In the figures, the bounds from d_{Hg} and d_D appear almost as horizontal lines. This results from the fact that for the $m_0 - m_{1/2}$ strips that we analyze, m_0 is almost proportional to $m_{1/2}$. Using dimensional analysis we can write

$$\tilde{d}_u - \tilde{d}_d \simeq k_1 \frac{\text{Im}[\mu] \text{ or Im}[a_0]}{m_{1/2}^3} \qquad d_e \simeq k_2 \frac{\text{Im}[\mu] \text{ or Im}[a_0]}{m_{1/2}^3}$$

where k_1 and k_2 are given by the relevant fermion masses and are independent of $m_{1/2}$. As a result, for a given value of $\tilde{d}_u - \tilde{d}_d$, $\text{Im}[\mu]$ (or $\text{Im}[a_0]$) itself is proportional to $m_{1/2}^3$ so d_e will not vary with $m_{1/2}$.

3) As discussed in ref. [45], at two-loop level, the imaginary a_0 can induce an imaginary correction to the Wino mass, giving rise to another contribution to the EDMs. In our analysis, we have taken this effect into account but it seems to be subdominant.

In the following, we will discuss what can be inferred about the sources of CPviolation from d_e and d_D if their values (or the bounds on them) turn out to be in certain ranges.

According to the figures 4–6, for $a_0 = 0$, any signal found by the Yale group implies that there are sources of CP-violation other than the phases of the Yukawa couplings. However, for larger values of a_0 , the effect of Y_{ν} on the EDMs can be observed by the Yale group within five years. According to figures 7–9, for $a_0 \gtrsim 1000 \text{ GeV}$ EDMs originating from complex Y_{ν} can be large enough to be observed by the Yale group. Therefore, if after five years the Yale group reports a null result, we can derive bounds on certain combinations of seesaw parameters and a_0 . At least it will be possible to discriminate between low and high a_0 values. If after five years the Yale group reports a null result, we can derive bounds on the seesaw parameters. However, if the Yale group finds that $10^{-31} \ e \ cm \ d_e \ 10^{-29} \ e \ cm$ we will not be able to determine whether d_e originates from complex Y_{ν} or from more familiar sources such as complex $a_0 \ or \ \mu$. To be able to make such a distinction, values of d_D down to $10^{-28} - 10^{-29}$ $e \ cm$ have to be probed which, at the moment, does not seem to be achievable.

If future searches for d_D find $d_D > 10^{-27} e$ cm but the Yale group finds $d_e < 2 \times 10^{-29} e$ cm (this can be tested within only 3 years of data taking by the Yale group [19]), we might conclude that the source of CP-violation is something other than pure Im[μ] or Im[a_0]; e.g., QCD θ -term which can give a significant contribution to d_D but only a negligible contribution to d_e . Another possibility is that there is a cancelation between the contributions of Im[μ] and Im[a_0] to d_e . The information on d_n would then help us to resolve this ambiguity provided that the theoretical uncertainties in calculation of d_n as well as d_D are sufficiently reduced.

On the other hand, if the Yale group detects $d_e > 2 \times 10^{-29} \ e$ cm, we will expect that $d_D > 10^{-27} \ e$ cm which will be a strong motivation for building a deuteron storage ring and searching for d_D . If such a detector finds a null result, within this framework the explanation will be quite non-trivial requiring some fine-tuned cancelation between different contributions.

According to these figures, in the foreseeable future, we will not be able to extract any information on the seesaw parameters from EDMs, because even if we develop techniques to probe d_e as small as $10^{-35} e - cm$, we will not be able to subtract (or dismiss) the effect coming from $\text{Im}[\mu]$ and $\text{Im}[a_0]$ unless we are able to probe $\tilde{d}_u - \tilde{d}_d$ at least 5 orders of magnitude below its present bound which seems impractical. Remember that this is under the optimistic assumptions that the mass of the lightest neutrino, m_1 , and $\text{Br}(\tau \to e\gamma)$ are close to their upper bounds and there is no cancelation between different contributions to the EDMs.

If, in the future, we realize that m_1 and $Br(\tau \to e\gamma)$ are indeed close to the present

upper bounds on them and $a_0 = 0$ ($a_0 = 1000$ GeV) but find $d_e < 10^{-35}e$ cm ($d_e < 10^{-34} e$ cm), we will be able to draw bounds on the phases of Y_{ν} which along with the information on the phases of the Dirac and Majorana phases of the neutrino mass matrix and the CP-violating phase of the left-handed slepton mass matrix may have some implication for leptogenesis. This is however quite an unlikely situation.

Let us now discuss the d_{μ} . As we saw in section 2, the phases of Y_{ν} manifest themselves in the d_{μ} through $\text{Im}[\Delta A_{\ell} \Delta m_{\tilde{L}}^2]_{\mu\mu}$ and $\text{Im}[\Delta m_{\tilde{E}}^2 m_{\ell}^2 \Delta m_{\tilde{L}}^2]_{\mu\mu}$. If a_0 is a real number, the matrix A_{ℓ} remains hermitean [13]. That is the radiative corrections due to Y_{ν} cannot induce nonzero $\text{Im}[\Delta A_{\ell}]_{ii}$. So, we can write

$$\operatorname{Im}[\Delta A_{\ell} \Delta m_{\tilde{L}}^2]_{\mu\mu} = \operatorname{Im}\left[(\Delta A_{\ell})_{\mu e} (\Delta m_{\tilde{L}}^2)_{e\mu}\right] + \operatorname{Im}\left[(\Delta A_{\ell})_{\mu\tau} (\Delta m_{\tilde{L}}^2)_{\tau\mu}\right]$$

and

$$\operatorname{Im}\left[\Delta m_{\tilde{E}}^2 m_{\ell}^2 \Delta m_{\tilde{L}}^2\right]_{\mu\mu} = \operatorname{Im}\left[(\Delta m_{\tilde{E}}^2)_{\mu e} m_e^2 (\Delta m_{\tilde{L}}^2)_{e\mu}\right] + \operatorname{Im}\left[(\Delta m_{\tilde{E}}^2)_{\mu\tau} m_{\tau}^2 (\Delta m_{\tilde{L}}^2)_{\tau\mu}\right].$$

The strong bounds on $\operatorname{Br}(\mu \to e\gamma)$ [18] and $\operatorname{Br}(\tau \to \mu\gamma)$ [41] can be translated into bounds on $(\Delta m_{\tilde{L}}^2)_{e\mu}$ and $(\Delta m_{\tilde{L}}^2)_{\tau\mu}$ as well as the corresponding elements of ΔA_{ℓ} . As a result, in the framework that imaginary Y_{ν} is the only source of CP-violation, we expect

$$d_{\mu} \sim d_e \frac{m_{\mu}}{m_e} \frac{(\Delta m_{\tilde{L}}^2)_{\tau\mu}}{(\Delta m_{\tilde{\tau}}^2)_{\tau e}} < 10^{-31} \ e \ \mathrm{cm},$$

which will not be observable even if the muon storage ring of a nu-factory is built [25]. On the other hand, imaginary a_0 and μ induce $d_{\mu} \sim d_e m_{\mu}/m_e$ and allow d_e to be as large as the experimental upper bound on it. In this case, we may have a chance of observing d_{μ} . Observing $d_{\mu} \gg m_{\mu} d_e/m_e$ will indicate that this simplified version of the MSSM is not valid.

5. Summary and conclusions

In this work we have studied EDMs of particles in the context of supersymmetric seesaw mechanism. We have examined various contributions to electron EDM induced by the CP-odd phases in the neutrino Yukawa matrix. Our analysis takes into account various contributions available in the literature as well as a new one, proportional to the gaugino masses, which is presented in eq. (2.5).

In our discussions we have first produced random complex neutrino Yukawa couplings consistent with the bounds from LFV rare decays and then calculated the electron EDM they induce along post-WMAP $m_0 - m_{1/2}$ strips for given values of $\tan \beta$ and a_0 [44]. We have found that, for small values of a_0 , the new contribution (2.5) can be dominant over the other contributions from Y_{ν} that had already been studied in the literature.

It turns out that for a realistic mass spectrum of supersymmetric particles, there is an extra suppression factor of $10^{-2} - 10^{-3}$ with which we would not encounter if all the supersymmetric masses were taken to be equal to each other. In figures 4–9, the values of d_e corresponding to different random complex Y_{ν} textures are represented by dots. For small values of $\tan \beta$ ($\tan \beta < 10$) and a_0 ($a_0 < 1000$ GeV), d_e induced by Y_{ν} is beyond the reach of the ongoing experiments [19]. Such values of d_e can however be probed by the proposed solid state based experiments [20]. For larger values of $\tan\beta$ and/or a_0 , the Yale group may be able to detect the effects of complex Y_{ν} on d_e . As it is demonstrated in figures 8 and 9, for $\tan \beta = 20$ and $a_0 = 1000 - 2000 \text{ GeV}$, a large fraction of parameter space yields d_e detectable by the Yale group. However, even in this case we will not be able to extract information on the seesaw parameters from d_e because the source of CPviolation might be a_0 and/or μ rather than Y_{ν} . If the future searches for d_D [34] find out that $d_D > 10^{-27} e$ cm then we will conclude that there is a source of CP-violation other than complex Y_{ν} . However, to prove that the dominant contribution to d_e detected by the Yale group comes from complex Y_{ν} hence to be able to extract information on the seesaw parameters from it- we should show that $d_D < 10^{-28} - 10^{-29} e$ cm which is beyond the reach of even the current proposals. Notice that for the purpose of discriminating between complex Y_{ν} and a_0/μ as sources of CP-violation, searching for d_{Hq} is not very helpful because mercury atom contains electron and hence d_{Hg} obtains a contribution from complex Y_{ν} . That is while ionized deuteron used for measuring d_D does not contain any electron and the contribution of complex Y_{ν} to it is negligible. To obtain information from d_n , the theoretical uncertainties first have to be resolved.

In this paper, we have also shown that for the neutrino Yukawa couplings satisfying the current bounds from the LFV rare decays, the electric dipole moment of muon induced by Y_{ν} is negligible and cannot be detected in the foreseeable future. Detecting a sizeable d_{μ} will indicate that there are sources of CP-violation beyond the complex Y_{ν} .

A. Appendix

Since d_D is dominantly given by $\tilde{d}_d - \tilde{d}_u$, in this section, we concentrate on evaluating \tilde{d}_q . One can repeat a similar discussion for d_q .

In section 2, we saw that integrating out N_i , the effects of CP-violating phases appear in the left-right mixing of sleptons which can be evaluated to $m_\ell m_{susy} F(Y_\nu, \text{Log}[M_{GUT}^2/M^2])/(16\pi^2)^2$ or for large tan β , to $m_\ell m_{susy} \tan \beta (m_\tau^2 \tan^2 \beta / v^2) F'(Y_\nu, \text{Log}[M_{GUT}^2/M^2])/(16\pi^2)^2$. For random Y_ν consistent with observed m_ν and bounds on the branching ratios of LFV rare decay, the functions F and F' take values smaller than 0.1. Since quarks do not directly couple to the leptonic sector, the CP-violation in the leptonic sector should be transferred to the quark sector through one-loop (or higher loop) effective operators made of Higgs and gauge bosons or their superpartners. To construct such an effective operator one more factor of Y_ℓ is needed to compensate for the left-right mixing mentioned above. Considering the fact that $Y_\tau \gg Y_\mu, Y_e$, the main contribution to the effective operator comes from the diagrams with τ and $\tilde{\tau}$ propagating in them. So the CP-odd effective potential will be given by

$$\frac{m_{\rm susy}^n m_{\tau}^2 \tan \beta F(Y_{\nu}, \log \left[M_{GUT}^2/M^2\right])}{(16\pi^2)^3}$$

or for large $\tan \beta$,

$$\frac{m_{\rm susy}^n m_{\tau}^2 \tan^2 \beta(m_{\tau}^2 \tan^2 \beta/v^2) F'(Y_{\nu}, \text{Log}[M_{GUT}^2/M^2])}{(16\pi^2)^3} \,.$$

In these formula, the power of m_{susy} , n, is determined by the dimension of the specific operator under consideration.

To evaluate d_q , we have to insert the CP-odd effective operator in another one-loop diagram. Since CEDMs mix left- and right-handed, the latter diagram should involve a factor of Y_q . So, we can write

$$\tilde{d}_q \sim \frac{Y_q g^2 g_s}{16\pi^2} \frac{m_\tau^2 \tan\beta F(Y_\nu, \log[M_{GUT}^2/M^2])}{(16\pi^2)^3 m_{\rm susy}^3}$$

and for large $\tan \beta$,

$$\tilde{d}_q \sim \frac{Y_q g^2 g_s}{16\pi^2} \frac{m_\tau^2 \tan^2 \beta (m_\tau^2 \tan^2 \beta / v^2) F'(Y_\nu, \text{Log}[M_{GUT}^2/M^2])}{(16\pi^2)^3 m_{\text{susy}}^3}.$$

As a result, we expect $\tilde{d}_d < 10^{-30}$ cm which cannot be observed even if the recent proposal [17] is implemented. We expect \tilde{d}_u to be even smaller because $Y_u/Y_d = m_u/m_d \cot \beta \ll 1$. Notice that although \tilde{d}_q is suppressed by a factor of $m_\tau^2 \tan^2 \beta/(16\pi^2 m_{susy}^2)$, $e\tilde{d}_d$ can be comparable to d_e . This originates from two facts: $Y_d/Y_e \sim 10$ and in the case of d_e , as we discussed in section 2, there is an extra suppression given by the functions $g(x_L, x_E)$ and $h(x_L, x_E)$. If we do precise two-loop calculation of \tilde{d}_d for a realistic SUSY spectrum, we may encounter similar suppression. As the above analysis show we do not expect an observable effect due to Y_{ν} in future searches for d_D and d_{Hg} so it seems there is not a strong motivation for performing such a complicated two-loop calculation.

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References

 see e.g., SUPER-KAMIOKANDE collaboration, M.B. Smy et al., Precise measurement of the solar neutrino day/night and seasonal variation in super-Kamiokande-I, Phys. Rev. D 69 (2004) 011104 [hep-ex/0309011];

SNO collaboration, S.N. Ahmed et al., Measurement of the total active B-8 solar neutrino flux at the sudbury neutrino observatory with enhanced neutral current sensitivity, Phys. Rev. Lett. **92** (2004) 181301 [nucl-ex/0309004];

SUPER-KAMIOKANDE collaboration, S. Moriyama, Super-Kamiokande atmospheric neutrinos, Nucl. Phys. 145 (Proc. Suppl.) (2005) 112.

- [2] KAMLAND collaboration, T. Araki et al., Measurement of neutrino oscillation with Kamland: evidence of spectral distortion, Phys. Rev. Lett. 94 (2005) 081801
 [hep-ex/0406035], http://www.awa.tohoku.ac.jp/KamLAND.
- [3] http://superk.physics.sunysb.edu/k2k/.
- [4] J. Bonn et al., The Mainz neutrino mass experiment, Nucl. Phys. 91 (Proc. Suppl.) (2001) 273.
- [5] U. Seljak et al., Cosmological parameter analysis including sdss ly-alpha forest and galaxy bias: constraints on the primordial spectrum of fluctuations, neutrino mass and dark energy, Phys. Rev. D 71 (2005) 103515 [astro-ph/0407372];
 SDSS collaboration, M. Tegmark et al., The 3D power spectrum of galaxies from the SDSS, Astrophys. J. 606 (2004) 702 [astro-ph/0310725];
 U. Seljak et al., Sdss galaxy bias from halo mass-bias relation and its cosmological implications, Phys. Rev. D 71 (2005) 043511 [astro-ph/0406594];
 V. Barger, D. Marfatia and A. Tregre, Neutrino mass limits from SDSS, 2DFGRS and WMAP, Phys. Lett. B 595 (2004) 55 [hep-ph/0312065].
- [6] A.Y. Smirnov, Alternatives to the seesaw mechanism, hep-ph/0411194.
- [7] T. Yanagida, Horizontal Gauge symmetry and masses of neutrinos, in Proceedings of the Workshop on the Baryon Number of the Universe and Unified Theories, Tsukuba, Japan, 13-14 Feb 1979;
 S. L. Glashow, The future of elementary particle physics, Based on lectures given at Cargese Summer Inst., Cargese, France, Jul 9-29, 1979, http://www.slac.stanford.edu/spires/find/hep/www?r=hutp-79-a059;
 M. Gell-Mann, P. Ramond and R. Slansky, Complex spinors and unified theories, http://www.slac.stanford.edu/spires/find/hep/www?r=print-80-0576;
 R.N. Mohapatra and G. Senjanovic, Neutrino mass and spontaneous parity nonconservation, Phys. Rev. Lett. 44 (1980) 912.
- [8] M. Fukugita and T. Yanagida, Baryogenesis without grand unification, Phys. Lett. B 174 (1986) 45.
- P. Nath, R. Arnowitt and A. H. Chamseddine, Applied N=1 supergravity, in Lectures given at Summer Workshop on Particle Physics, Trieste, Italy, Jun 20 - Jul 29, 1983, http://www.slac.stanford.edu/spires/find/hep/www?r=nub-2613.
- [10] F. Borzumati and A. Masiero, Large muon and electron number violations in supergravity theories, Phys. Rev. Lett. 57 (1986) 961.
- [11] S. Davidson and A. Ibarra, Determining seesaw parameters from weak scale measurements?, JHEP 09 (2001) 013 [hep-ph/0104076].
- [12] J. Hisano, D. Nomura and T. Yanagida, Atmospheric neutrino oscillation and large lepton flavour violation in the SUSY SU(5) GUT, Phys. Lett. B 437 (1998) 351 [hep-ph/9711348]; A. Romanino and A. Strumia, Electron and muon electric dipoles in supersymmetric scenarios, Nucl. Phys. B 622 (2002) 73 [hep-ph/0108275]; J.R. Ellis, J. Hisano, M. Raidal and Y. Shimizu, Lepton electric dipole moments in non-degenerate supersymmetric seesaw models, Phys. Lett. B 528 (2002) 86 [hep-ph/0111324];
 I. Masina, Lepton electric dipole moments from heavy states Yukawa couplings, Nucl. Phys. B 671 (2003) 432 [hep-ph/0304299].

- [13] Y. Farzan and M.E. Peskin, The contribution from neutrino Yukawa couplings to lepton electric dipole moments, Phys. Rev. D 70 (2004) 095001 [hep-ph/0405214].
- B. Dutta and R.N. Mohapatra, Lepton electric dipole moments, supersymmetric seesaw and leptogenesis phase, Phys. Rev. D 68 (2003) 113008 [hep-ph/0307163];
 I. Masina and C.A. Savoy, On power and complementarity of the experimental constraints on seesaw models, Phys. Rev. D 71 (2005) 093003 [hep-ph/0501166].
- [15] M.E. Pospelov and I.B. Khriplovich, Electric dipole moment of the W boson and the electron in the Kobayashi-Maskawa model, Sov. J. Nucl. Phys. 53 (1991) 638.
- [16] Y. Farzan, Effects of the neutrino B-term on slepton mixing and electric dipole moments, Phys. Rev. D 69 (2004) 073009 [hep-ph/0310055].
- [17] EDM collaboration, Y.K. Semertzidis et al., A new method for a sensitive deuteron EDM experiment, AIP Conf. Proc. 698 (2004) 200-204 [hep-ex/0308063].
- [18] PARTICLE DATA GROUP collaboration, S. Eidelman et al., Review of particle physics, Phys. Lett. B 592 (2004) 1.
- [19] D. Kawall et al., electron in AIP Conf. Proc. 698 (2004) 192.
- [20] S.K. Lamoreaux, Solid state systems for electron electric dipole moment and other fundamental measurements, nucl-ex/0109014.
- [21] J.J. Hudson, B.E. Sauer, M.R. Tarbutt and E.A. Hinds, Measurement of the electron electric dipole moment using YBF molecules, Phys. Rev. Lett. 89 (2002) 023003 [hep-ex/0202014];
 Y.K. Semertzidis, Electric dipole moments of fundamental particles, Nucl. Phys. 131 (Proc. Suppl.) (2004) 244 [hep-ex/0401016].
- [22] P.G. Harris et al., New experimental limit on the electric dipole moment of the neutron, Phys. Rev. Lett. 82 (1999) 904.
- [23] http://p25ext.lanl.gov/edm/edm.htmlhttp://p25ext.lanl.gov/edm/edm.html.
- [24] Y.K. Semertzidis et al., Sensitive search for a permanent muon electric dipole moment, hep-ph/0012087.
- [25] J. Aysto et al., Physics with low-energy muons at a neutrino factory complex, hep-ph/0109217.
- [26] M.V. Romalis, W.C. Griffith and E.N. Fortson, A new limit on the permanent electric dipole moment of HG-199, Phys. Rev. Lett. 86 (2001) 2505 [hep-ex/0012001].
- [27] T. Ibrahim and P. Nath, The neutron and the electron electric dipole moment in N = 1 supergravity unification, Phys. Rev. D 57 (1998) 478 [hep-ph/9708456].
- [28] J. Hisano and Y. Shimizu, Hadronic edms induced by the strangeness and constraints on supersymmetric CP phases, Phys. Rev. D 70 (2004) 093001 [hep-ph/0406091].
- [29] M. Pospelov and A. Ritz, Neutron edm from electric and chromoelectric dipole moments of quarks, Phys. Rev. D 63 (2001) 073015 [hep-ph/0010037].
- [30] T. Falk, K.A. Olive, M. Pospelov and R. Roiban, MSSM predictions for the electric dipole moment of the HG-199 atom, Nucl. Phys. B 560 (1999) 3 [hep-ph/9904393].

- [31] J. Hisano, M. Kakizaki, M. Nagai and Y. Shimizu, Hadronic EDMs in SUSY SU(5) guts with right-handed neutrinos, Phys. Lett. B 604 (2004) 216 [hep-ph/0407169];
 T. Falk, K.A. Olive, M. Pospelov and R. Roiban, MSSM predictions for the electric dipole moment of the HG-199 atom, Nucl. Phys. B 560 (1999) 3 [hep-ph/9904393].
- [32] M. Pospelov, Best values for the CP-odd meson nucleon couplings from supersymmetry, Phys. Lett. B 530 (2002) 123 [hep-ph/0109044].
- [33] M. Pospelov and A. Ritz, Electric dipole moments as probes of new physics, Ann. Phys. (NY) 318 (2005) 119 [hep-ph/0504231].
- [34] O. Lebedev, K.A. Olive, M. Pospelov and A. Ritz, Probing CP-violation with the deuteron electric dipole moment, Phys. Rev. D 70 (2004) 016003 [hep-ph/0402023].
- [35] J. Hisano and Y. Shimizu, Hadronic edms induced by the strangeness and constraints on supersymmetric CP phases, Phys. Rev. D 70 (2004) 093001 [hep-ph/0406091].
- [36] J.R. Ellis, J. Hisano, M. Raidal and Y. Shimizu, A new parametrization of the seesaw mechanism and applications in supersymmetric models, Phys. Rev. D 66 (2002) 115013 [hep-ph/0206110].
- [37] S. Hannestad, Neutrino masses and the dark energy equation of state: relaxing the cosmological neutrino mass bound, astro-ph/0505551.
- [38] S. Antusch, J. Kersten, M. Lindner and M. Ratz, Running neutrino masses, mixings and CP phases: analytical results and phenomenological consequences, Nucl. Phys. B 674 (2003) 401 [hep-ph/0305273].
- [39] M. Pospelov, Best values for the CP-odd meson nucleon couplings from supersymmetry, Phys. Lett. B 530 (2002) 123 [hep-ph/0109044].
- [40] O. Lebedev, K.A. Olive, M. Pospelov and A. Ritz, Probing CP-violation with the deuteron electric dipole moment, Phys. Rev. D 70 (2004) 016003 [hep-ph/0402023].
- [41] BABAR collaboration, B. Aubert et al., Search for lepton flavor violation in the decay $\tau \rightarrow \mu\gamma$, Phys. Rev. Lett. **95** (2005) 041802 [hep-ex/0502032].
- [42] K. Hayasaka et al., Search for $\tau \to e \gamma$ decay at belle, Phys. Lett. B 613 (2005) 20 [hep-ex/0501068].
- [43] S.T. Petcov, S. Profumo, Y. Takanishi and C.E. Yaguna, Charged lepton flavor violating decays: leading logarithmic approximation versus full RG results, Nucl. Phys. B 676 (2004) 453 [hep-ph/0306195].
- [44] L.S. Stark, P. Hafliger, A. Biland and F. Pauss, New allowed mSUGRA parameter space from variations of the trilinear scalar coupling a0, JHEP 08 (2005) 059 [hep-ph/0502197].
- [45] K.A. Olive, M. Pospelov, A. Ritz and Y. Santoso, CP-odd phase correlations and electric dipole moments, Phys. Rev. D 72 (2005) 075001 [hep-ph/0506106].