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## ABSTRACT

Exploring gate insulator materials for 2D transistors and their defect properties is of importance for device performance optimization. In this work, the structural and electronic properties of intrinsic vacancies in the  $\text{CaF}_2$  single layer and its heterostructures with monolayer  $\text{MoS}_2$  are investigated from first-principles calculations.  $V_{\text{Ca}}$  introduces a shallow defect level close to the VBM, whereas  $V_{\text{F}}$  introduces a deep level below the CBM. In both cases, spin polarization is observed. Overall,  $V_{\text{F}}$  has a relatively lower formation energy than  $V_{\text{Ca}}$ , except for the extreme Ca-rich case. Thus,  $V_{\text{F}}$  should be dominant in  $\text{CaF}_2$ . The band offset between  $\text{CaF}_2$  and  $\text{MoS}_2$  is determined to be type-I, with large offsets at both the conduction band and valence band. With the presence of vacancies in  $\text{CaF}_2$ , the type-I band offset is preserved. The electron or hole on the defect states will transfer from  $\text{CaF}_2$  to  $\text{MoS}_2$  due to the large band offset, and spin polarization vanishes. Nevertheless, there are no defect states inside the gap or around the band edge of  $\text{MoS}_2$ , and the electronic properties of  $\text{MoS}_2$  are almost intact. Compared with  $h$ -BN that has a small valence band offset with  $\text{MoS}_2$  and could introduce in-gap defect states,  $\text{CaF}_2$  can be a good candidate to serve as the dielectric layer of  $\text{MoS}_2$ -based transistors.

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## I. INTRODUCTION

Semiconducting transition metal dichalcogenides (TMDs) have been extensively investigated due to their electronic, optical, and mechanical properties<sup>1–5</sup> as well as their combinations with other two-dimensional crystals<sup>6–9</sup> which led to an emergence of a new class of artificial materials with unique properties. Such combinations are used in the design of field-effect transistors (FETs),<sup>10–16</sup> which are useful to overcome the limitations of Si technologies by achieving small channel geometries. Among these, FETs based on  $\text{MoS}_2$  have been attracting attention due to low sub-threshold swing values and high on/off current ratios.<sup>10,11</sup> Although  $\text{MoS}_2$  shows extraordinary results in FETs, the selection of a gate insulator greatly affects the performance of such devices. It is reported that materials such as  $\text{SiO}_2$  or  $\text{Al}_2\text{O}_3$  expose various problems in such systems due to their amorphous phase and numerous defects in their crystal structures.<sup>17,18</sup> In order to overcome such problems, a well-known single-layer insulator hexagonal boron nitride ( $h$ -BN) with a wide bandgap of 5.765 eV<sup>19</sup> is employed in numerous

FET structures.<sup>20–23</sup> Although there are promising results, the small out-of-plane dielectric constant of  $h$ -BN that deteriorates the electronic transport properties<sup>24,25</sup> and band offset with similar VBM levels<sup>26</sup> limits the performance of the FET structures. In addition, it is reported that in  $\text{MoS}_2/h$ -BN heterostructures, the presence of intrinsic defects in the  $h$ -BN layer creates defect states either inside the bandgap or close to the band edge of  $\text{MoS}_2$ ,<sup>20</sup> which could trap the carriers in the devices. Therefore, the competitive 2D insulator to serve as the dielectric layer of  $\text{MoS}_2$ -based FETs remains to be explored.

Calcium fluoride ( $\text{CaF}_2$ ) has been investigated in various fields. Due to its transparency over a wide spectrum of optical frequencies,  $\text{CaF}_2$  is an important material in infrared spectroscopy.<sup>27–29</sup> Applications of  $\text{CaF}_2$  extend to a wide range of areas such as laser architecture<sup>30,31</sup> and dentistry.<sup>32,33</sup> Encouraged by such promising results in various fields, thin films of  $\text{CaF}_2$  have been studied since the 1990s.<sup>34–36</sup> It is reported that  $\text{CaF}_2$  thin films can be used for superlattice,<sup>37</sup> diode,<sup>38</sup> chemical sensors,<sup>39</sup> and transistors.<sup>34</sup> Most recently, the  $\text{CaF}_2$  sheet with about 2 nm thickness is used in the design of a

competitive FET based on bilayer MoS<sub>2</sub>.<sup>26,40</sup> Low subthreshold swings value of 90 mV dec<sup>-1</sup> and high on/off current ratios up to 10<sup>7</sup> were realized. In previous works, single-layer CaF<sub>2</sub> in the 1T structure is theoretically predicted, and its dynamical stability and insulating characteristic with a wide bandgap of 9.49 eV<sup>41,42</sup> are reported. Given the excellent properties of two-dimensional CaF<sub>2</sub>, it is expected to be an appealing material in nanoscale heterojunction and substrate applications that complements the widely used *h*-BN.

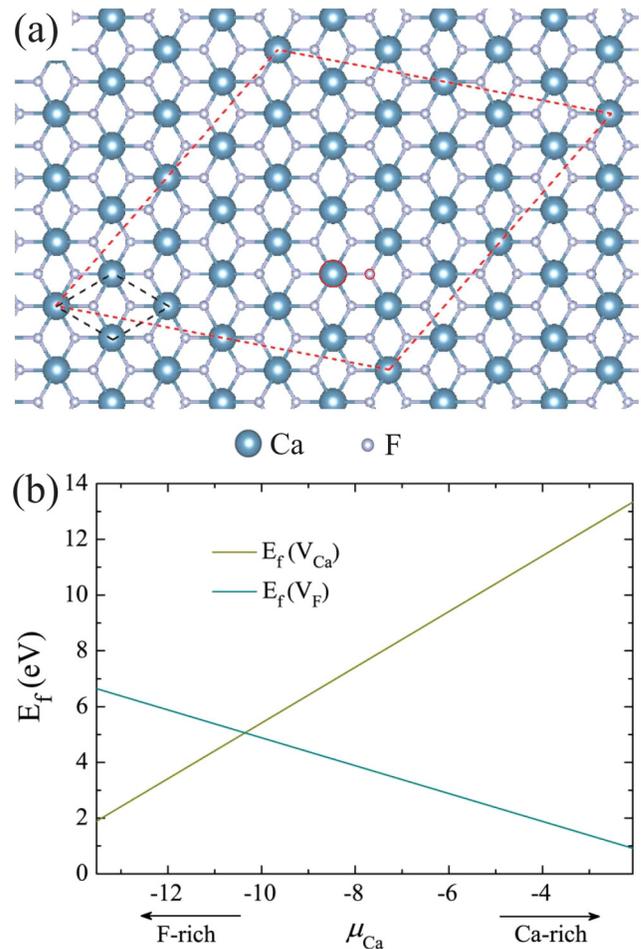
In this article, using *ab initio* calculations, the monolayer MoS<sub>2</sub> heterostructures with monolayer CaF<sub>2</sub> are predicted, and it is revealed that type-I heterojunction is formed<sup>43</sup> with large band offsets. Furthermore, the effects of intrinsic fluorine and calcium vacancies on the CaF<sub>2</sub> layer and the CaF<sub>2</sub>/MoS<sub>2</sub> heterostructure are investigated. It is found that in single-layer CaF<sub>2</sub>, V<sub>F</sub> introduces a deep level below the CBM, whereas V<sub>Ca</sub> introduces a shallow level at the VBM. In both cases, spin polarization around the vacancy sites is observed. In CaF<sub>2</sub>/MoS<sub>2</sub> heterostructures, the electron or hole on V<sub>F</sub> or V<sub>Ca</sub> defect states will transfer from CaF<sub>2</sub> to MoS<sub>2</sub> due to the large band offset, and the spin polarization vanishes. Nevertheless, there are no defect states inside the gap or around the band edge of MoS<sub>2</sub>, and the electronic properties of monolayer MoS<sub>2</sub> is almost intact. Thus, CaF<sub>2</sub> can have potential applications for the dielectric layer of MoS<sub>2</sub>-based FETs.

This article is organized as follows: In Sec. II, the details of the computational method and the simulations are given. The results are given in Sec. III and the regarding discussion is supplied about the work in three parts. In Sec. III A, the behavior of calcium and fluorine vacancies in 1T-CaF<sub>2</sub> crystals, in Sec. III B the pure CaF<sub>2</sub>/MoS<sub>2</sub> heterostructure, and in Sec. III C the V<sub>F</sub> and V<sub>Ca</sub> defects in the CaF<sub>2</sub>/MoS<sub>2</sub> heterostructure are discussed. The results are concluded in Sec. IV.

## II. COMPUTATIONAL METHOD

The calculations have been performed using density functional theory (DFT) within the Vienna *ab initio* simulation package (VASP).<sup>44,45</sup> The projected augmented wave (PAW) potential<sup>46</sup> is used to describe the ion and core electrons. The exchange-correlation functional is treated by the generalized gradient approximation (GGA) of Perdew–Burke–Ernzerhof (PBE),<sup>47</sup> and the van der Waals (vdW) corrections are taken into account by the D3 scheme of Grimme.<sup>48</sup> The kinetic energy cutoff of the plane-wave basis set is 600 eV, and the geometries are optimized with the conjugate gradient method. The criteria for the total energy convergence during self-consistent calculation is 10<sup>-5</sup> eV. Spin-orbit interactions are taken into account in the electronic band structure calculations.

The single-layer CaF<sub>2</sub> is simulated by a (2, 4) × (6, -2) × 1 supercell [the lattice parameter of its primitive cell is  $a_{\text{CaF}_2} = 3.60$  Å, as shown in Fig. 1(a)] to discuss the behavior of defects. We model the CaF<sub>2</sub>/MoS<sub>2</sub> heterostructures by stacking the above CaF<sub>2</sub> layer on top of a 6 × 6 × 1 supercell of single-layer MoS<sub>2</sub> ( $a_{\text{MoS}_2} = 3.16$  Å). The lattice mismatch between the two layers is about 0.34 %, and it consists of 192 atoms in the simulation cell. When introducing one defect per cell, we optimize the atomic positions until the remaining atomic forces are less than 0.01 eV/Å and fix the cell parameters at the value of 18.96 Å of the MoS<sub>2</sub> supercell. A vacuum layer larger



**FIG. 1.** (a) Crystal structures of pristine 1T-CaF<sub>2</sub>. Its primitive cell is given by the black dashed line and the (2, 4) × (6, -2) × 1 supercell is marked by the red dashed line. The single Ca or F vacancies in the CaF<sub>2</sub> monolayer are marked by red circles. (b) The formation energies of V<sub>Ca</sub> and V<sub>F</sub> defects in CaF<sub>2</sub> as a function of chemical potential  $\mu_{\text{Ca}}$ .

than 20 Å is also introduced to minimize interactions between periodic images.

The formation energies ( $E_f$ ) of vacancies defects ( $V_i$ ) in CaF<sub>2</sub> are calculated as follows:<sup>49</sup>

$$E_f(V_i) = E(V_i) - E(\text{CaF}_2) + \sum_i n_i \mu_i, \quad (1)$$

where  $E(\text{CaF}_2)$  and  $E(V_i)$  are the total energies of the perfect and defective systems of CaF<sub>2</sub>,  $n_i$  is the number of vacant atoms of type  $i$ , and  $\mu_i$  is the chemical potential of element  $i$ . One can define the relative chemical potential  $\Delta\mu_i = \mu_i - \mu_i^0$  ( $\mu_i^0$  is the chemical potential of element  $i$  in its most stable elemental phase), which

meet the boundary conditions

$$\begin{aligned}\Delta\mu_{\text{Ca}} &\leq 0, \\ \Delta\mu_{\text{F}} &\leq 0, \\ \Delta\mu_{\text{Ca}} + 2\Delta\mu_{\text{F}} &= \Delta H_f(\text{CaF}_2),\end{aligned}\quad (2)$$

where  $\Delta H_f(\text{CaF}_2)$  is the formation enthalpy of  $\text{CaF}_2$ . Thus, we obtain the formation energies of  $V_i$  defects in  $\text{CaF}_2$  as a function of chemical potential  $\mu_{\text{Ca}}$  and allowed range of  $\mu_{\text{Ca}}$ ,

$$\begin{aligned}E_f(V_{\text{Ca}}) &= E(V_{\text{Ca}}) - E(\text{CaF}_2) + \mu_{\text{Ca}}, \\ E_f(V_{\text{F}}) &= E(V_{\text{F}}) - \frac{E(\text{CaF}_2) + \mu_{\text{Ca}}}{2}, \\ \Delta H_f(\text{CaF}_2) + \mu_{\text{Ca}}^0 &\leq \mu_{\text{Ca}} \leq \mu_{\text{Ca}}^0.\end{aligned}\quad (3)$$

### III. RESULTS AND DISCUSSION

#### A. The behavior of calcium and fluorine vacancies in 1T- $\text{CaF}_2$ crystals

The native defects are always generated during crystal growth and such imperfections in the periodic lattice structure directly lead to the alteration of the electronic and magnetic properties of the system more or less. Therefore, investigation of defects is of great importance. We first investigate the structural and electronic behavior of the native vacancy defects, namely,  $V_{\text{Ca}}$  and  $V_{\text{F}}$ , in the 1T- $\text{CaF}_2$  crystal.

When a single Ca vacancy is introduced in the  $\text{CaF}_2$  monolayer [Fig. 1(a)], its nearby F atoms move away from the vacancy site after structural relaxation, resulting in a 0.05 Å reduction of Ca-F bond length compared with the defect-free case. This is possibly caused by Coulomb repulsion between these negatively charged F atoms. The formation energy of  $V_{\text{Ca}}$  as a function of Ca chemical potential is shown in Fig. 1(b), and the value is about 13.34 eV under Ca-rich condition, smaller than the value of 13.75 eV in crystalline  $\text{CaF}_2$ .<sup>50</sup> Under F-rich condition, the formation energy decreases to 2.07 eV. The density of states (DOS) of  $V_{\text{Ca}}$  is plotted in Fig. 2(a). It is seen that  $V_{\text{Ca}}$  does not introduce the in-gap defect state. Moreover, while the up-spin states in the valence band are fully occupied, the down-spin states near the VBM are partially unoccupied. These states are mainly contributed by fluorine atoms around vacancy [Fig. 2(c)]. Therefore, the calcium vacancy introduces a magnetic moment of  $2\mu_B$  with spin polarization mainly localized on fluorine atoms surrounding the vacancy [Fig. 2(b)].

Meanwhile, the fluorine vacancy causes the slight displacement of calcium atoms around vacancy. The formation energy is about 6.64 eV under F-rich condition and 0.92 eV under Ca-rich condition (Fig. 1). Overall, the formation energy of  $V_{\text{F}}$  is smaller than that of  $V_{\text{Ca}}$ , except for the F-rich region ( $\mu < -10.49$  eV), suggesting that the  $V_{\text{F}}$  defect is more likely to exist in the  $\text{CaF}_2$  layer. Experiments showed that the major defect in the  $\text{CaF}_2$  crystal is the  $V_{\text{F}}$ -related anti-Frenkel defect.<sup>51</sup> Moreover, other theoretical calculations also reveal higher formation energy of Ca vacancies

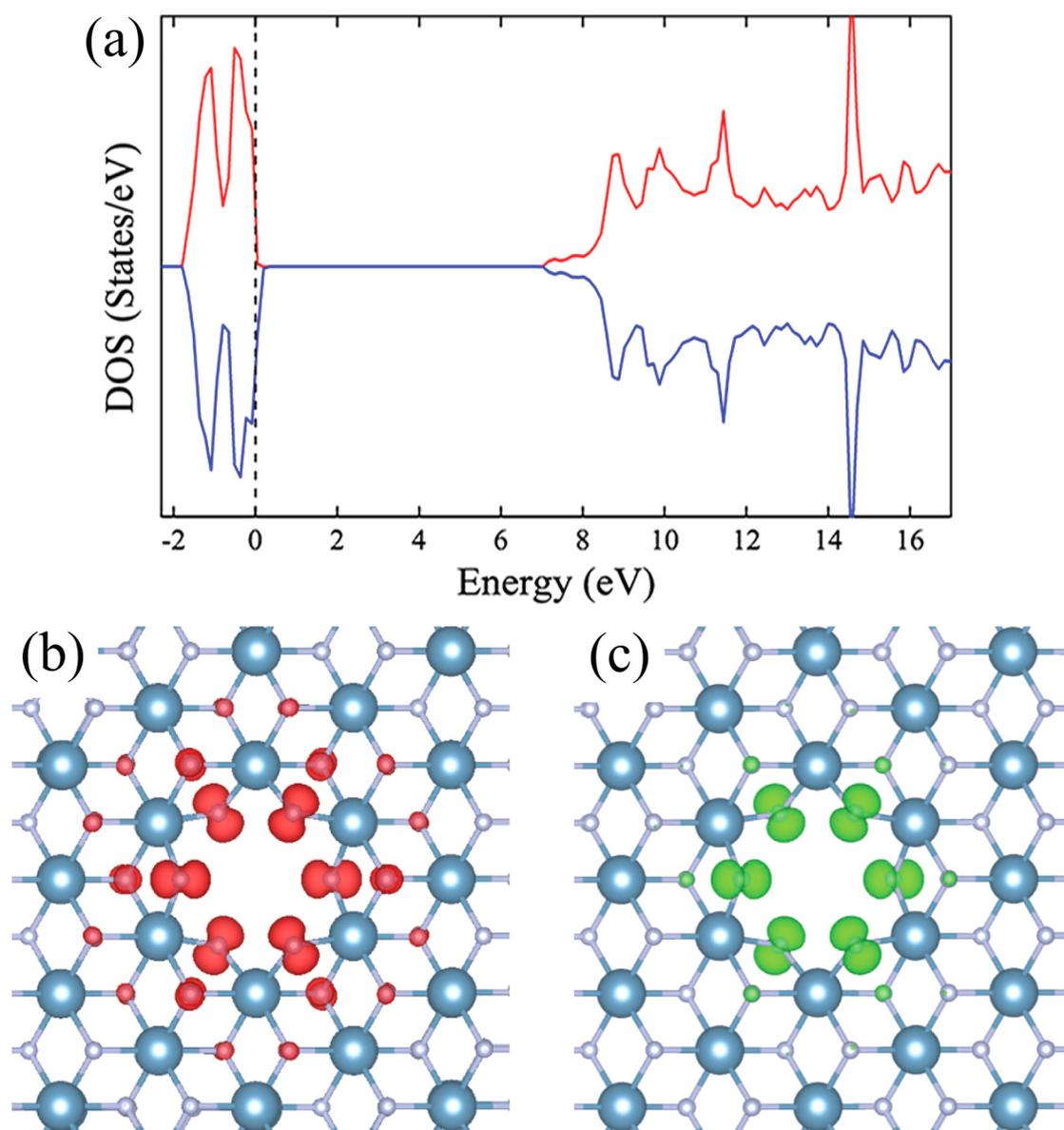
compared to F vacancies.<sup>50,52</sup> These observations are consistent with our results. The corresponding density of states is shown in Fig. 3.  $V_{\text{F}}$  introduces a defect level inside the bandgap, with its spin-up component fully occupied while the spin-down component empty. Thus, we obtain a spin-polarized ground state with a magnetic moment of  $1\mu_B$  and the spin polarization is localized at the position of vacancy [Fig. 3(a)]. The charge density distribution of the defect levels is presented in Figs. 3(c) and 3(d), and it indicates that the defect levels are mainly contributed by F vacancies.

When the multiple point defects exist in the structures, it will exhibit ferromagnetic (FM) and anti-ferromagnetic (AFM) states. Here, magnetism caused by F defect pair is investigated by comparing defect formation energies as a function of neighboring distance. The second F defect is formed by removing the F atom at the sites displayed in Fig. 4(a). In single  $\text{CaF}_2$  layers with F defect pairs, FM and AFM phases exhibit  $2\mu_B$  and  $0\mu_B$  net magnetic moments, respectively, which are reflected in the corresponding spin densities presented in Figs. 4(b)–4(f). The formation energy of the second F vacancy at different sites under the F-rich and the Ca-rich conditions is shown in Fig. 4(g). It is obtained that second F vacancy located in site 1 has the lowest formation energy in the AFM state and highest energy in the FM state, and the corresponding energy difference is 145 meV [Figs. 4(g) and 4(h)]. In the AFM case, the formation energies of 6.53 eV under the F-rich condition and 0.81 eV under the Ca-rich condition are also smaller than that of the single  $V_{\text{F}}$  case, indicating that the  $V_{\text{F}}$  defects tend to form neighboring pairs in the AFM state. With the increasing distance between F vacancies, the energy differences between FM and AFM states decrease (17, 4, and 1 meV at site 2, 3, and 4, respectively). This phenomenon is caused by attraction (repulsion) forces between neighboring defects in the AFM (FM) phase. Furthermore, the magnetic ground state caused by defect pair formation remains as AFM. When the second F defect is located at site 5, the energy difference between FM and AFM phases becomes negligible, indicating that the interaction between neighboring defects is very weak with large enough distance. We have also analyzed the DOS of a single  $V_{\text{F}}$  and a neighboring  $V_{\text{F}}$  pair and found their defect state energy is quite similar, and the difference is less than 0.08 eV. For simplicity, we will use a single  $V_{\text{F}}$  model in heterostructure calculation.

#### B. Pure $\text{CaF}_2/\text{MoS}_2$ heterostructure

Now we discuss the properties of the defect-free heterostructure of a  $\text{CaF}_2$  monolayer stacked on the  $\text{MoS}_2$  monolayer. After structural relaxation, the average distance between fluorine and sulfur atomic layers in the interstitial region is about 3.06 Å, as shown in Fig. 5. The Ca-F and Mo-S bond lengths are 2.285 and 2.408 Å, respectively.

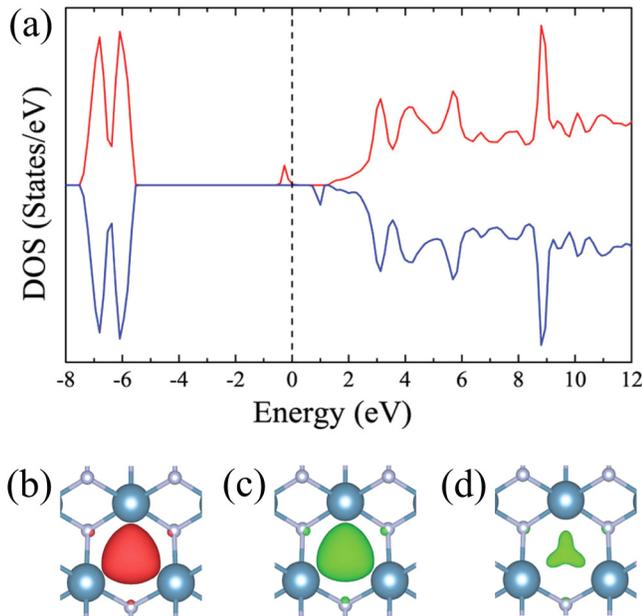
To clearly understand the electronic properties of the  $\text{CaF}_2/\text{MoS}_2$  heterostructure, we first give the electronic band structures of isolated layers of  $\text{CaF}_2$  and  $\text{MoS}_2$  (Fig. 6). With PBE-D3 calculations, we obtain an indirect bandgap of 7.09 eV for  $\text{CaF}_2$ , compared with other theoretical value of 7.17 eV.<sup>41</sup> For  $\text{MoS}_2$ , a direct bandgap of 1.66 eV is given, which is close to the other calculated value of 1.75 eV,<sup>20</sup> and the valence top and the conduction bottom are located at the K point. To identify the type of  $\text{CaF}_2/\text{MoS}_2$



**FIG. 2.** (a) The spin-polarized density of states and (b) spin density for the  $V_{Ca}$  defect in the  $CaF_2$  monolayer. The fermi energy in (a) is set at zero. Here, red color in the spin density plot represents the spin-up channel, and there is no net spin-down contribution. (c) The sum of the partial charge densities (in green) for the states in the energy range of 0–0.5 eV (as well as in other relevant figures). It is contributed by unoccupied spin-down states. The isosurface level of charge density is set to 0.002 e/Bohr<sup>3</sup>.

heterostructure, we compare the band alignment of  $CaF_2$  and  $MoS_2$  by aligning the vacuum levels and find that the valence-band edge has lower energy in  $CaF_2$  than that of  $MoS_2$  while the conduction-band edge shows a opposite trend [Fig. 6(b)], suggesting  $CaF_2/MoS_2$  to be a type I (straddling gap) heterojunction.<sup>43</sup> If Anderson's rule is applicable (i.e., the charge transfer and interlayer interaction are negligible), then the valence band offset (VBO) can

be estimated as 3.01 eV, and the conduction band offset (CBO) can be estimated as 2.42 eV. Using the hybrid functional HSE06 method,<sup>53</sup> the valance and conduction-band offsets of  $CaF_2$  and  $MoS_2$  increase by 1.03 and 0.29 eV [Fig. 6(c)]. According to the HSE06 calculation, the bandgap of monolayer  $MoS_2$  is 2.31 eV. We also performed  $G_0W_0$  calculation and found a larger quasi-particle gap of 2.95 eV, consistent with previous studies.<sup>54</sup> On the other



**FIG. 3.** (a) The spin-polarized density of states and (b) spin density for the  $V_F$  defect in the  $\text{CaF}_2$  monolayer. The Fermi energy in (a) is set at zero. Here, red color in the spin density plot represents the spin-up channel, and there is no net spin-down contribution. (c)–(d) The sum of the partial charge densities (in green) in the range of (c)  $-1$  to  $0$  eV and (d)  $0.5$  to  $1.1$  eV. They are contributed by isolated occupied spin-up states and unoccupied spin-down states, respectively. The isosurface level is set to  $0.0055$  e/Bohr<sup>3</sup>.

hand, the calculated  $G_0W_0$  gap for monolayer  $\text{CaF}_2$  is  $12.48$  eV, which is  $3.42$  eV larger than the HSE06 result. Thus, the band offset between  $\text{CaF}_2$  and  $\text{MoS}_2$  is likely to be underestimated even by HSE06. Nevertheless, the type of band alignment and the large band offset values should not be qualitatively affected by the choice of PBE, HSE06, or  $G_0W_0$ . In addition, it should have no significant influence on our prediction after two subsystems' combination since the corresponding band offset is large enough.

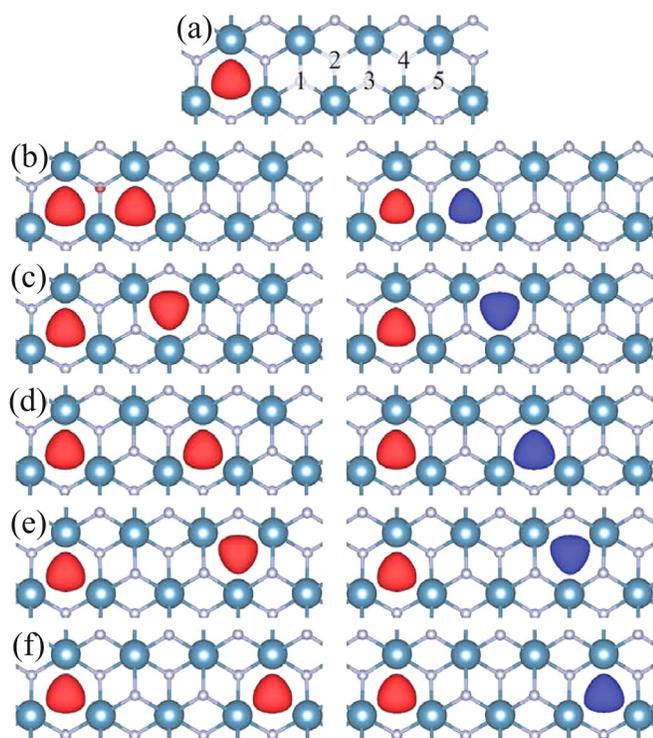
To further verify the type-I band offset, the partial density of states (PDOS) of the  $\text{CaF}_2/\text{MoS}_2$  heterostructure is calculated using PBE-D3, as shown in Fig. 7. The result confirmed the predicted type-I character of the  $\text{CaF}_2/\text{MoS}_2$  heterostructure. Through the band alignment, we obtain that the eigenvalues of the band edges of  $\text{CaF}_2$  relative to that of  $\text{MoS}_2$  move about  $0.3$  eV to higher energy after the formation of the heterostructure. Such a shift indicates the formation of a small interface dipole due to charge transfer from  $\text{MoS}_2$  to  $\text{CaF}_2$ . Nevertheless, the VBO ( $2.60$  eV) and the CBO ( $2.75$  eV) remain large. To explore possible hybridization-induced self-energy correction, we also performed HSE06 calculation for the  $\text{MoS}_2/\text{CaF}_2$  heterostructure supercell and found that the VBO and CBO are  $4.03$  and  $3.05$  eV, which is only slightly modified compared to the prediction from Anderson's rule [Fig. 6(c)]. Considering the underestimation of bandgap due to the use of PBE and HSE06, the actual band offsets would be even higher. It is interesting to note

that with either PBE or HSE06, we observed an  $\sim 0.07$  eV reduction in the bandgap of  $\text{MoS}_2$ . The gap reduction could possibly be contributed by the dielectric screening effect<sup>55</sup> of the  $\text{CaF}_2$ , and such effect is typically a few tens of meV for TMDs.<sup>56</sup> Experimentally,  $h$ -BN is often adopted as the dielectric layer of electronic devices based on 2D materials. However, although  $h$ -BN also has a type-I band offset with  $\text{MoS}_2$ ,<sup>20,57</sup> their VBO is quite small ( $\sim 0.1$  eV), which can lead to large gate leakage currents. Therefore, on the basis of band offset,  $\text{CaF}_2$  is more suitable to serve as the dielectric layer of  $\text{MoS}_2$ -based transistors than  $h$ -BN.

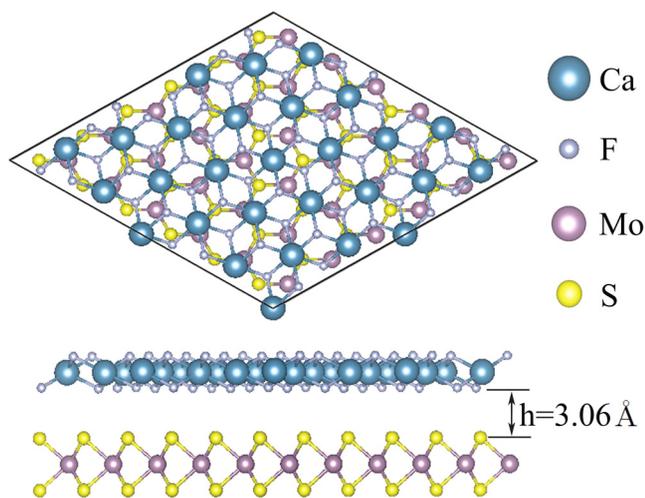
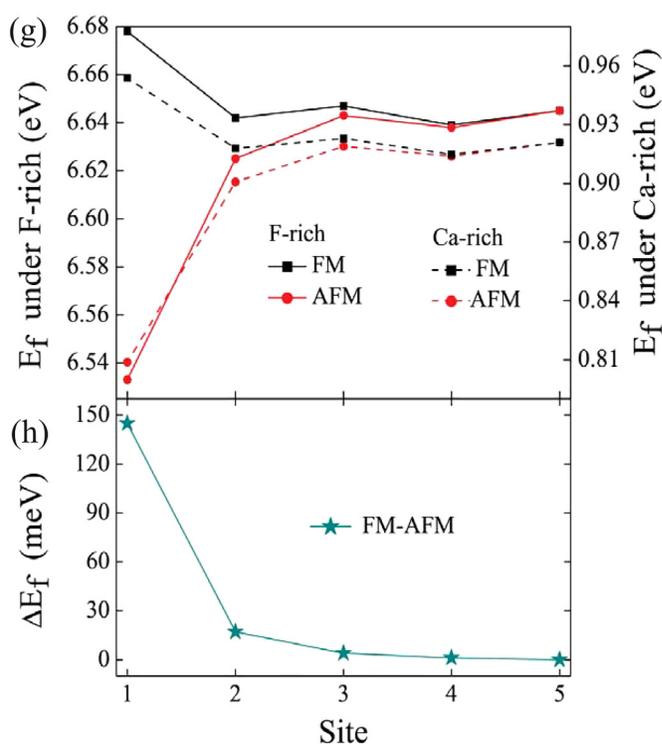
### C. The behavior of $V_{\text{Ca}}$ and $V_{\text{F}}$ defects in $\text{CaF}_2/\text{MoS}_2$ heterostructure

Intrinsic defect properties of the dielectric layer in transistors can greatly affect the device performance. In this section, we investigate the effects of  $V_{\text{Ca}}$  and  $V_{\text{F}}$  defects on  $\text{CaF}_2/\text{MoS}_2$  heterostructures. Considering the two layers of F atoms in the heterostructure, there could be two types of  $V_{\text{F}}$ . One is located at the heterostructure interface (denoted as  $V_{\text{F-d}}$ ), and the other one is located at the outer surface (denoted as  $V_{\text{F-u}}$ ). The removal of a fluorine atom from the  $\text{CaF}_2$  layer leads to a significant change for geometry. As the fluorine and calcium atoms around vacancies move outward relative to the position of vacancy, they also move toward the interstitial region between the layers due to the existence of the  $\text{MoS}_2$  layer. The Ca–F bond length is  $0.07$  Å longer for  $V_{\text{F-u}}$  defect than that of defect-free heterostructure defect while  $0.04$  Å longer for  $V_{\text{F-d}}$  defect. In the case of  $V_{\text{Ca}}$  defect, geometry distortion is smaller. The Ca–F bond lengths around the vacancies are about  $0.1$  Å shorter than the defect-free case, similar to the  $V_{\text{Ca}}$  defect in the isolated  $\text{CaF}_2$  layer.

Figure 8 plots the density of states for  $V_{\text{F-u}}$ ,  $V_{\text{F-d}}$ , and  $V_{\text{Ca}}$  defects in the  $\text{CaF}_2/\text{MoS}_2$  heterostructure. With the presence of  $\text{MoS}_2$  layer, the defect state close to the conduction-band edge caused by fluorine vacancy in the  $\text{CaF}_2$  layer vanishes [Figs. 8(a) and 8(b)], and spin polarization also disappears. The Fermi levels in the  $V_{\text{F-u}}$  and  $V_{\text{F-d}}$  cases are both located at the conduction-band edge of the  $\text{MoS}_2$  layer, and the valence-band offset increases by  $0.41$  eV for  $V_{\text{F-u}}$  defect and  $0.17$  eV for  $V_{\text{F-d}}$  defect compared to the defect-free case. According to Fig. 3(a), the  $V_{\text{F}}$  defect level is about  $1$  eV lower than the CBM of  $\text{CaF}_2$ , while the CBO between  $\text{CaF}_2$  and  $\text{MoS}_2$  is  $2.75$  eV. Hence, the defect level is much higher than the CBM of  $\text{MoS}_2$ , and the electron occupying the defect level in  $\text{CaF}_2$  will transfer to the conduction band of  $\text{MoS}_2$ , with the Fermi level shifted to the conduction band edge of  $\text{MoS}_2$ . Such a defect-induced indirect doping is also observed in the  $\text{MoS}_2/\text{BN}$  heterostructure.<sup>20</sup> The situation for  $V_{\text{Ca}}$  is similar [Fig. 8(c)], except for that the transferred carrier is hole. Due to the large VBO between  $\text{MoS}_2$  and  $\text{CaF}_2$ , the Fermi level crosses the valence band edge of  $\text{MoS}_2$ , and four fully occupied defect states occur above the valence-band top of the  $\text{CaF}_2$  subsystem. There is also no magnetism. Moreover, the band offset is modified by Ca vacancy, with about  $1.12$  eV reduction (increase) in VBO (CBO). The charge density of the states for the  $V_{\text{F-u}}$  and  $V_{\text{F-d}}$  cases at the conduction band below the Fermi level is shown in Figs. 8(d) and 8(e) and that for the  $V_{\text{Ca}}$  case at the valence band above the Fermi level is shown in Fig. 8(f). It is seen that these states mainly locate on the  $\text{MoS}_2$



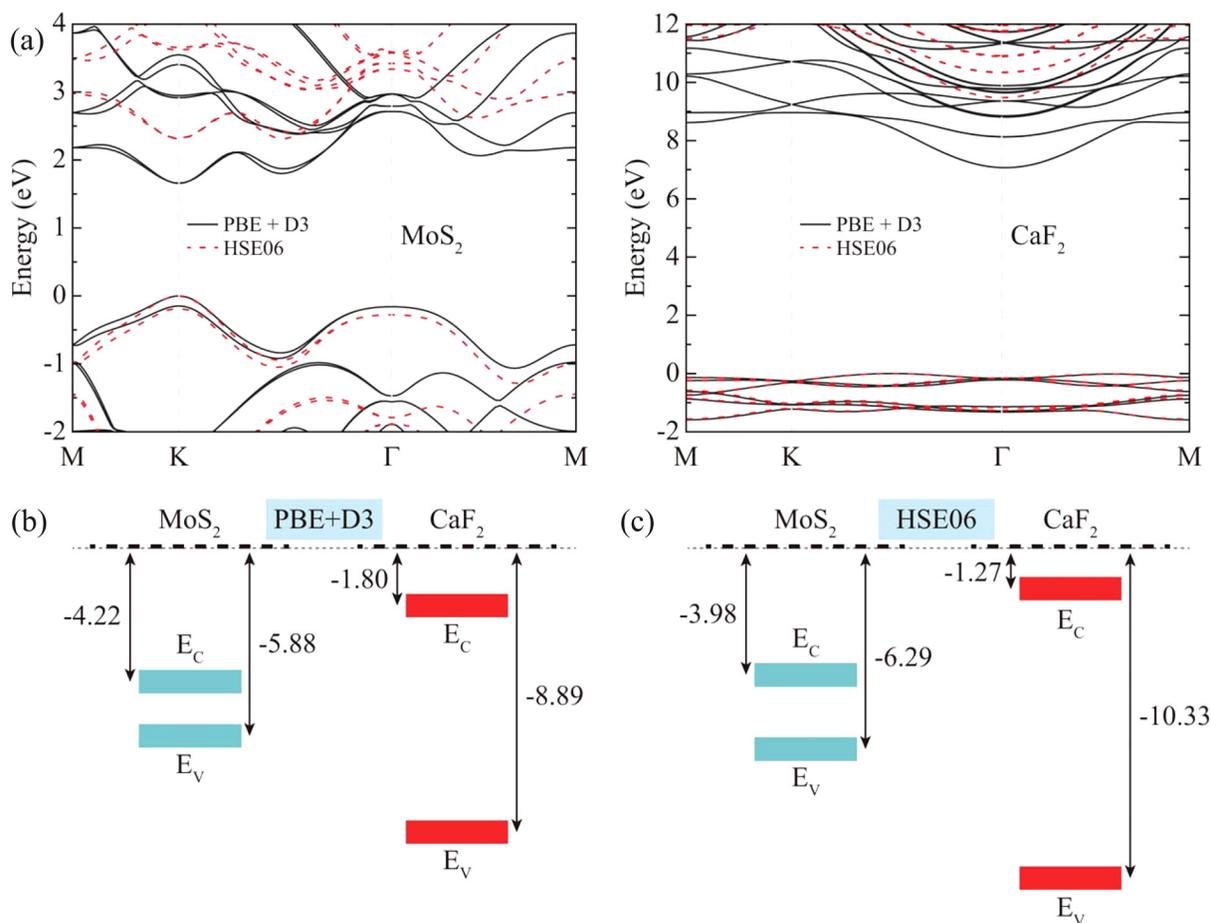
**FIG. 4.** (a) The possible F vacancy sites 1, 2, 3, 4, and 5 for the formation of defect pair in  $\text{CaF}_2$  with single F vacancy. The spin density of F defect pairs with FM and AFM phases where the second F vacancy is located at sites (b) 1, (c) 2, (d) 3, (e) 4, and (f) 5. Red or blue represents spin-up or spin-down channel here. The isosurface level is set to  $0.007 \text{ e/Bohr}^3$ . (g) The formation energy of second F vacancies under F-rich and Ca-rich conditions and (h) energy differences at five sites.



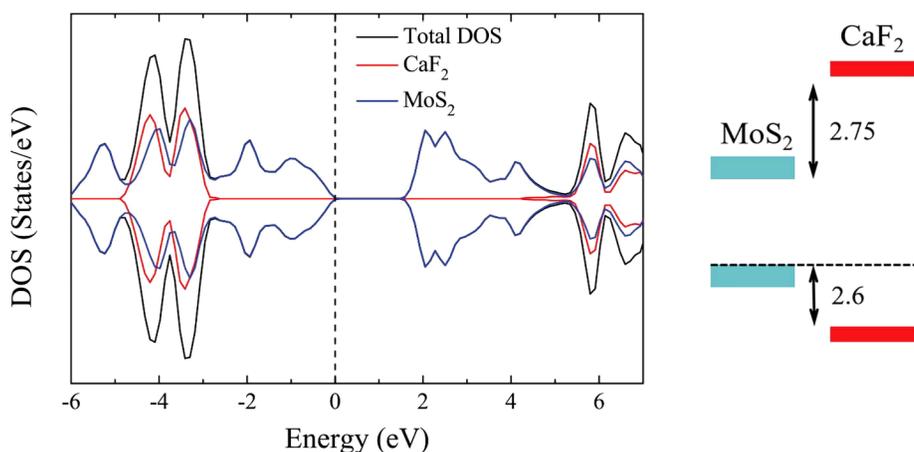
**FIG. 5.** The top and side views of  $\text{CaF}_2/\text{MoS}_2$  heterostructure. Its simulated cell is constructed by stacking a  $(2, 4) \times (6, -2) \times 1$  supercell of  $\text{CaF}_2$  on a  $6 \times 6 \times 1$  supercell of  $\text{MoS}_2$ .

layer and are quite delocalized, leading to the disappearance of magnetism. Previous studies revealed that in the  $\text{MoS}_2/h\text{-BN}$  heterostructure, vacancies in  $h\text{-BN}$  creates defect states either close to the band edge of  $\text{MoS}_2$  or inside its bandgap;<sup>20</sup> thus, the carrier transport in  $\text{MoS}_2$  may be affected by these defect states. In the case of  $\text{MoS}_2/\text{CaF}_2$  heterostructure, the vacancies in  $\text{CaF}_2$  do not introduce defect states inside the gap or around the band edge. Comparing Figs. 7 and 8(a)–8(c), it is seen that when interfaced with defective  $\text{CaF}_2$ , the DOS of the  $\text{MoS}_2$  layer are quite similar to the case in a perfect heterostructure, indicating the effect of vacancies to the electronic structure of the  $\text{MoS}_2$  layer is minor. Such a defect insensitivity, combined with a proper band offset, makes  $\text{CaF}_2$  a good candidate for the dielectric layer of  $\text{MoS}_2$ -based transistors.

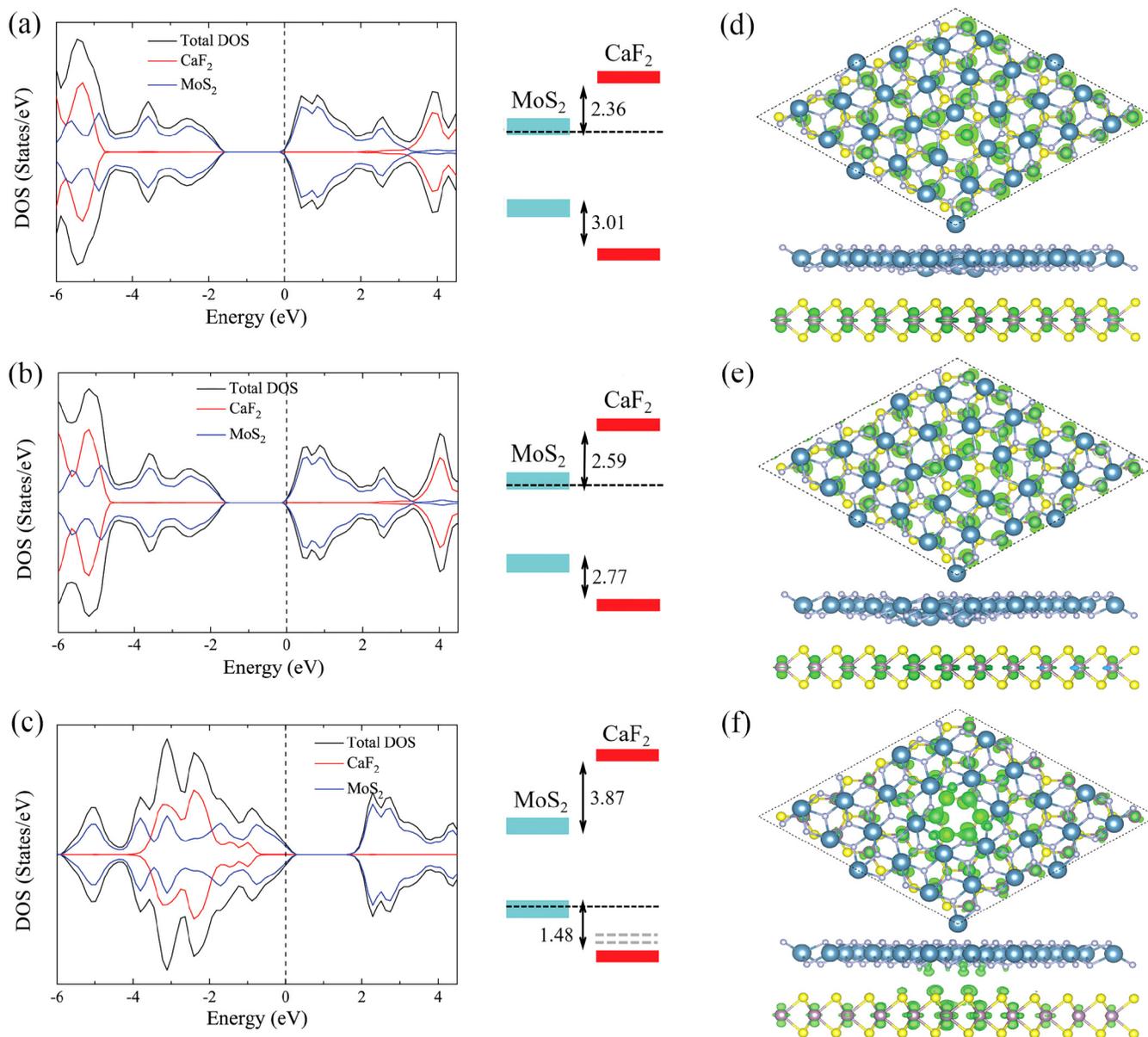
It is worth to mention that the FET made in experiments consists of  $\sim 2 \text{ nm}$  thick  $\text{CaF}_2$  and bilayer  $\text{MoS}_2$ ,<sup>26,40</sup> while in our calculation, monolayers are used. To explore the possible thickness effect, we have calculated the band structures of 5-layer  $\text{CaF}_2$  and bilayer  $\text{MoS}_2$ . The bandgap of 5-layer  $\text{CaF}_2$  and bilayer  $\text{MoS}_2$  is 6.80 and 1.23 eV, which are smaller than our calculated data of monolayer  $\text{CaF}_2$  (7.09 eV) and  $\text{MoS}_2$  (1.66 eV), respectively. The VBO or CBO between  $\text{CaF}_2$  and  $\text{MoS}_2$  multi-layers is 2.93 or 2.64 eV, which is



**FIG. 6.** (a) Electronic band structures of MoS<sub>2</sub> and CaF<sub>2</sub> calculated by PBE-D3 method and HSE06 method<sup>59</sup> with spin-orbit coupling. The bandgap of MoS<sub>2</sub> and CaF<sub>2</sub> is 1.66 and 7.09 eV by PBE-D3 method and 2.31 and 9.06 eV by HSE06 method, respectively. For comparison, the valence-band maximum is set to be zero of energy by shifting the band structures. The band alignment of MoS<sub>2</sub> and CaF<sub>2</sub> using (b) PBE-D3 method and (c) HSE06 method. The vacuum energies are set to zero.



**FIG. 7.** The spin-resolved partial density of states (PDOS) and band alignment of the CaF<sub>2</sub>/MoS<sub>2</sub> heterostructure. The Fermi level is set to zero. The bandgap of MoS<sub>2</sub> and CaF<sub>2</sub> in the heterostructure is 1.59 and 6.96 eV by the PBE-D3 method, respectively.



**FIG. 8.** The spin-resolved partial density states and band alignment of (a)  $V_{F-u}$ , (b)  $V_{F-d}$ , and (c)  $V_{Ca}$  defects in  $CaF_2/MoS_2$  heterostructures. The Fermi energy is located at zero with a black dashed line. The gray dashed line in (c) denotes the defect levels. The top and side views of band-decomposed charge density distributions of the conduction band in the energy range of  $-0.5$  to  $0$  eV for (d)  $V_{F-u}$  and (e)  $V_{F-d}$  defects and (f) the valence band in the energy range of  $0-0.5$  eV for  $V_{Ca}$  defect. The isosurface level is set to  $0.00007$  e/Bohr<sup>3</sup> in (d) and (e) and  $0.001$  e/Bohr<sup>3</sup> in (f).

close to the value of  $3.01$  or  $2.42$  eV for the monolayer case. Therefore, our results remain valid for systems using thicker films. Moreover, the control of a FET is achieved through a gate electric field (the magnitude is typically less or comparable to  $0.1$  V/Å). To explore the electric field effect, we have calculated the properties of

the  $CaF_2/MoS_2$  monolayer heterostructure under the electric field of  $0.1$  and  $-0.1$  V/Å. It is found that the change in the VBO and CBO is within  $\sim 0.1$  eV. Therefore, at an experimentally achievable strength, the gate electric field should have minor effect on the electronic states on the  $CaF_2/MoS_2$  heterostructure.

#### IV. CONCLUSION

In conclusion, the structural and electronic properties of the intrinsic vacancies in an isolated  $\text{CaF}_2$  layer and  $\text{CaF}_2/\text{MoS}_2$  heterostructures are investigated from first-principles calculations. The removal of fluorine or calcium atom from the isolated  $\text{CaF}_2$  layer induces spin polarization around vacancies with magnetic moment of  $1\mu_B$  or  $2\mu_B$ , respectively.  $V_{\text{Ca}}$  introduces a shallow defect level close to the VBM, whereas  $V_{\text{F}}$  introduces a deep level below the CBM. Overall,  $V_{\text{F}}$  has a relatively lower formation energy than  $V_{\text{Ca}}$ , except for the extremely Ca-rich case. Thus,  $V_{\text{F}}$  should be dominant in  $\text{CaF}_2$ . The magnetic coupling between the fluorine vacancy pair is also studied, and it is found that the nearest-neighbor pair with AFM configuration is favorable due to the lower formation energy. The band offset between  $\text{CaF}_2$  and  $\text{MoS}_2$  is determined to be type-I, with large CBO and VBO. With the presence of vacancies in  $\text{CaF}_2$ , the type-I band offset is maintained. The electron or hole on the defect states will transfer from  $\text{CaF}_2$  to  $\text{MoS}_2$  due to the large band offset, and spin polarization vanishes. Nevertheless, there are no defect states inside the gap or around the band edge of  $\text{MoS}_2$ , and the electronic properties of  $\text{MoS}_2$  are almost intact. Compared with *h*-BN that has a small VBO with  $\text{MoS}_2$  and could introduce in-gap defect states,  $\text{CaF}_2$  can be a good candidate to serve as the dielectric layer of  $\text{MoS}_2$ -based transistors.

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#### DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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