



## Full Length Article

# First-principles investigation of structural, Raman and electronic characteristics of single layer Ge<sub>3</sub>N<sub>4</sub>

Y.O. Yayak<sup>a</sup>, Y. Sozen<sup>b</sup>, F. Tan<sup>b</sup>, D. Gungen<sup>a</sup>, Q. Gao<sup>c</sup>, J. Kang<sup>c</sup>, M. Yagmurcukardes<sup>b,d,e,\*</sup>, H. Sahin<sup>b</sup>

<sup>a</sup> Department of Chemistry, Izmir Institute of Technology, 35430 Izmir, Turkey

<sup>b</sup> Department of Photonics, Izmir Institute of Technology, 35430 Izmir, Turkey

<sup>c</sup> Beijing Computational Science Research Center, Beijing 100193, China

<sup>d</sup> Department of Physics, University of Antwerp, Groenenborgerlaan 171, B-2020 Antwerp, Belgium

<sup>e</sup> NANOLab Center of Excellence, Groenenborgerlaan 171, B-2020 Antwerp, Belgium



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## A B S T R A C T

By means of density functional theory-based first-principle calculations, the structural, vibrational and electronic properties of single-layer Ge<sub>3</sub>N<sub>4</sub> are investigated. Structural optimizations and phonon band dispersions reveal that single-layer ultrathin form of Ge<sub>3</sub>N<sub>4</sub> possesses a dynamically stable buckled structure with large hexagonal holes. Predicted Raman spectrum of single-layer Ge<sub>3</sub>N<sub>4</sub> indicates that the buckled holey structure of the material exhibits distinctive vibrational features. Electronic band dispersion calculations indicate the indirect band gap semiconducting nature of single-layer Ge<sub>3</sub>N<sub>4</sub>. It is also proposed that single-layer Ge<sub>3</sub>N<sub>4</sub> forms type-II vertical heterostructures with various planar and puckered 2D materials except for single-layer GeSe which gives rise to a type-I band alignment. Moreover, the electronic properties of single-layer Ge<sub>3</sub>N<sub>4</sub> are investigated under applied external in-plane strain. It is shown that while the indirect gap behavior of Ge<sub>3</sub>N<sub>4</sub> is unchanged by the applied strain, the energy band gap increases (decreases) with tensile (compressive) strain.

## 1. Introduction

Group-IV nitrides have drawn attention because of their easy accessibility, low-cost preparation, chemical stability and electrically tunability. Germanium nitride (Ge<sub>3</sub>N<sub>4</sub>), a member of group-IV nitrides, has been widely studied for a long time and was first experimentally realized by reacting metallic germanium and ammonia gas at high temperatures in 1930 [1]. After that, various experimental methods have been developed in order to synthesize different phases of Ge<sub>3</sub>N<sub>4</sub> [2–6]. While the cubic phase of Ge<sub>3</sub>N<sub>4</sub> was synthesized using laser-heated diamond anvil cell [3], its  $\gamma$ -phase was demonstrated by controlling the pressure and temperature in  $\alpha$ - and  $\beta$ -phases [4].

The electronic and optical properties of the synthesized phases of bulk Ge<sub>3</sub>N<sub>4</sub>, which are large-gap semiconductors, have been studied by means of theoretical simulations [7–12]. Molina et al. investigated the properties of five different phases of Ge<sub>3</sub>N<sub>4</sub> and  $\beta$ -Ge<sub>3</sub>N<sub>4</sub> was reported to be the most stable phase among them [7]. Spinel germanium nitrides can be considered as multifunctional materials with their large exciton binding energies and tunable band gaps [11]. Among  $\alpha$ -,  $\beta$ -, and  $\gamma$ -Ge<sub>3</sub>N<sub>4</sub>

phases, the  $\beta$ -Ge<sub>3</sub>N<sub>4</sub> was reported to be a direct band gap semiconductor [12]. In addition, the thermal conductivity of  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> and  $\gamma$ -Ge<sub>3</sub>N<sub>4</sub> were studied by comparing to that of  $\beta$ -Si<sub>3</sub>N<sub>4</sub> and it was shown that both  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> and  $\gamma$ -Ge<sub>3</sub>N<sub>4</sub> exhibit higher thermal conductivity at room temperature with less anisotropy [13]. In another study, both experimental and computational methods were used in order to investigate the potential of group-IV nitrides as optoelectronic materials and it was found that the Ge<sub>3</sub>N<sub>4</sub> has lower electron effective masses compared to that of  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> [14–18]. Moreover, Maeda et al. reported that ultrathin Ge<sub>3</sub>N<sub>4</sub> was used to create Ag/Ge<sub>3</sub>N<sub>4</sub>/Ge metal–insulator–semiconductor device that exhibits capacitance–voltage characteristics with no hysteresis [15]. The properties of Au/Ge<sub>3</sub>N<sub>4</sub>/Ge capacitors were also studied and it was found that the gate leakage current density is lower compared to that of poly-Si/SiO<sub>2</sub>/Si while being thermally stable at higher temperatures [16]. Other applications of Ge<sub>3</sub>N<sub>4</sub> includes solar cell design and photocatalyst in water splitting process. It was also proposed that adsorption of RuO<sub>2</sub> to  $\beta$ -Ge<sub>3</sub>N<sub>4</sub> surface created a non-oxide photocatalysts for overall water splitting as oxygen evolution reaction occurs on the surface of  $\beta$ -Ge<sub>3</sub>N<sub>4</sub> whereas hydrogen evolution reaction tends to

\* Corresponding author at: Department of Physics, University of Antwerp, Groenenborgerlaan 171, B-2020 Antwerp, Belgium.

E-mail address: [mehmetyagmurcukardes.edu@gmail.com](mailto:mehmetyagmurcukardes.edu@gmail.com) (M. Yagmurcukardes).

occur on RuO<sub>2</sub> [19]. Enhancement by ammonia treatment of the photocatalytic activity of  $\beta$ -Ge<sub>3</sub>N<sub>4</sub> in water splitting process was reported [20]. Recently, a solar cell design was proposed where spinel Ge<sub>3</sub>N<sub>4</sub> and Si<sub>3</sub>N<sub>4</sub> were used as solar cell absorber materials [21].

Over the last two decades, low-dimensional materials have been paid a lot of attention in material science and engineering. The discovery of graphene was thought to be a milestone in science [22], and various graphene-like 2D materials, such as transition metal dichalcogenides (TMDs) [23–32], Xenes [33–39], hexagonal boron nitride (h-BN) [40] have been added to the 2D family. In order to produce smaller devices, thin, stable, durable and electrically tunable materials are required. Although, various nanostructural forms of germanium nitrides, such as nanobelts, have been reported in the sizes of 30 to 300 nm in width both in  $\alpha$ -Ge<sub>3</sub>N<sub>4</sub> and  $\beta$ -Ge<sub>3</sub>N<sub>4</sub> phases [41–43], its 2D single-layer form has not been investigated to date.

In this work, two-dimensional form of Ge<sub>3</sub>N<sub>4</sub> was investigated by means of *ab initio* calculations. The rest of the paper is organized as follows; Computational methodology is given in Section 2. Structural properties are given in Section 3.1. Vibrational properties are discussed in Section 3.2. In addition, results of the electronic properties are presented in Section 3.3 and strain-dependent electronic band dispersions are given in Section 3.4. Lastly, we concluded our results in Section 4.

## 2. Computational Methodology

First-principles calculations were performed based on density functional theory (DFT) as implemented the Vienna *ab initio* Simulation Package (VASP) [44,45]. For the exchange–correlation functional, Generalized Gradient Approximation (GGA) in the form of Perdew-Burke-Ernzerhof (PBE) was considered [46]. The projector augmented wave (PAW) potentials were used as pseudopotential datasets [47]. The van der Waals (vdW) interaction was included in the form of DFT-D2 method of Grimme [48]. Bader technique was employed to investigate the charge transfer between atoms [49].

The kinetic energy cutoff and the convergence criterion for the total energy was set to 520 eV and 10<sup>−5</sup> eV, respectively. 15 Å vacuum spacing was inserted in order to avoid adjacent layer-layer interactions in the z-axis. For the structural optimization of the primitive unit cell, a 5 × 5 × 1 k-point mesh was used, and it was doubled for accurate density of states calculations. In order to achieve the fully relaxed structure, pressures on each direction of the unit cell was reduced below 1 kBar. The Heyd-Scuseria-Ernzerhof (HSE06) functional was employed so as to estimate experimental electronic band structure better [50]. The cohesive energy per atom was calculated using the below;

$$E_{Coh} = \frac{n_{Ge}E_{Ge} + n_N E_N - E_{sys}}{n_{tot}} \quad (1)$$

where  $n_{Ge}$  is the number of Ge atoms in the system,  $n_N$  is the number of N atoms in the system,  $n_{tot}$  is the total number of atoms in the system,  $E_{Ge}$  is the energy of a single Ge atom,  $E_N$  is the energy of a single N atom and  $E_{sys}$  is the total energy of the system.

The vibrational properties were investigated via PHON code, which uses the small displacement method [51]. For the investigation of Raman activities of phonon modes, we calculated the polarizability of crystal lattice by taking the derivative of the macroscopic dielectric tensor with respect to the finite-difference method [52].

In order to simulate STM images, partial charge densities of the primitive unit cell in the range [−3,0] eV were calculated, results were postprocessed by using Equation 2 which is based on STM working principles and employed in our recent works [53–55].

$$E_{total} = \sum_n^h E_n e^{-kz_n} \quad (2)$$

where  $E_{total}$  is the summed charge density matrix,  $n$  is the array element

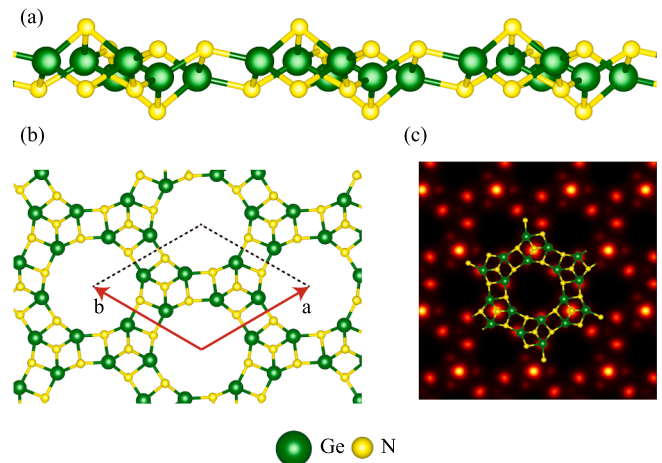
in z-axis,  $h$  is the total number of array elements in z-axis,  $E_n$  is the partial charge density matrix for the  $n^{th}$  array element,  $k$  is a constant, and  $z_n$  is the distance from the artificial STM tip in the z direction. 2D array  $E_{total}$  is converted into 8-bit image, 4 × 4 average filter is applied in order to improve the image quality, and visualized using custom colormap.

## 3. Results

### 3.1. Structural Properties

Crystal structure of the single-layer Ge<sub>3</sub>N<sub>4</sub>, which is shown in Fig. 1, is formed by a primitive unit cell containing six germanium and eight nitrogen atoms. As viewed from the side perspective, Ge<sub>3</sub>N<sub>4</sub> contains two Ge-atomic layers and four N-atomic layers forming a buckled structure. The corresponding space group symmetry of single layer Ge<sub>3</sub>N<sub>4</sub> is  $P-3$ . The optimized in-plane lattice parameter of Ge<sub>3</sub>N<sub>4</sub> is  $\vec{a} = \vec{b} = 8.16$  Å. The corresponding Ge-N bond lengths are found to vary between 1.85 and 2.03 Å. Moreover, the thickness of single-layer Ge<sub>3</sub>N<sub>4</sub>, defined as the distance between the outer-most N atoms, is found to be 2.79 Å. In order to have a better understanding on single layer Ge<sub>3</sub>N<sub>4</sub>, the results are compared with those for single layer C<sub>3</sub>N<sub>4</sub>, another member of 2D nitrate family. The optimized lattice parameter of Ge<sub>3</sub>N<sub>4</sub> (8.16 Å) is found to be larger than that of g-C<sub>3</sub>N<sub>4</sub> (7.15 Å) as a consequence of longer Ge-N bonds. Indeed, such larger bond length and lattice parameter result in smaller cohesive energy for single layer Ge<sub>3</sub>N<sub>4</sub> indicating less energetic stability of the structure [56]. Note that, a detailed information about the atomic positions and the optimized structure is given in the Supplementary Information. Bader analysis shows that single-layer Ge<sub>3</sub>N<sub>4</sub> structure is formed such that each Ge atom donates 1.8 e<sup>−</sup> while each N atom receives 1.3 e<sup>−</sup> charge, indicating ionic bond character in the structure. Furthermore, the cohesive energy ( $E_{Coh}$ ) is found to be 4.08 eV/atom. As compared to well-known 2D materials, such as graphene (10.04 eV/atom) and MoS<sub>2</sub> (9.53 eV/atom), single-layer Ge<sub>3</sub>N<sub>4</sub> has a much lower cohesive energy indicating its less energetic stability [57]. In addition on the other hand, the cohesive energy of Ge<sub>3</sub>N<sub>4</sub> is lower than that of predicted single-layer nitrides, BN (8.83 eV/atom), AlN (7.15 eV/atom), GaN (6.37 eV/atom), and InN (5.47 eV/atom) [57]. Furthermore, the work function of Ge<sub>3</sub>N<sub>4</sub> is calculated to be higher than that of g-C<sub>3</sub>N<sub>4</sub> (6.38 eV for Ge<sub>3</sub>N<sub>4</sub> and 4.82 eV for g-C<sub>3</sub>N<sub>4</sub>) [58] stating that the electrons are mostly localized in single layer Ge<sub>3</sub>N<sub>4</sub> and it is chemically more stable than g-C<sub>3</sub>N<sub>4</sub> in terms of the electron exchange from the layer.

Mechanical properties of single-layer Ge<sub>3</sub>N<sub>4</sub> are calculated in terms of its in-plane stiffness ( $C$ ) and the Poisson ratio ( $\nu$ ). The calculated in-



**Fig. 1.** For the single-layer of Ge<sub>3</sub>N<sub>4</sub>; (a) Side and (b) top views of the crystal structure. (c) The simulated STM image.

plane stiffness of single-layer  $\text{Ge}_3\text{N}_4$  is 62 N/m. As compared to the stiffness of well-known single-layers such as  $\text{MoS}_2$  (122 N/m) [59] and graphene (340 N/m) [60], single-layer  $\text{Ge}_3\text{N}_4$  is a soft material. On the other hand, while the stiffness of  $\text{Ge}_3\text{N}_4$  is lower than that of other nitrides (267, 116, and 110 N/m for BN, AlN, and GaN, respectively), it is comparable to that of InN (67 N/m) [57]. In addition, the Poisson ratio of a material, which is the measure of expansion perpendicular to the direction of compression, has to be between  $-1$  to  $0.5$  for a stable, linear elastic material [61]. The Poisson ratio of single-layer  $\text{Ge}_3\text{N}_4$  is found to be 0.24 and it is between that of  $\text{MoS}_2$  (0.26) [59] and graphene (0.19) [60]. As compared to planar single-layers of nitrides, Poisson ratio of  $\text{Ge}_3\text{N}_4$  is higher than that of BN (0.21) while it is much smaller than Poisson ratio of AlN (0.46), GaN (0.48), and InN (0.59) indicating mechanical stability of  $\text{Ge}_3\text{N}_4$  over other nitride single-layers [57]. In addition, as compared to that of  $g\text{-C}_3\text{N}_4$  (0.23), the Poisson ratio of  $\text{Ge}_3\text{N}_4$  is almost the same which can be related to the crystal structure similarity [56].

### 3.2. Vibrational Properties

In this section, we extend our predictions by confirming the dynamical stability and investigating the lattice dynamics of the free-standing  $\text{Ge}_3\text{N}_4$  crystal structure through the phonon band spectrum calculations. In order to obtain phonon branches, force constant matrix is generated by the implementation of small displacement method. It is seen that all phonon branches display completely positive phonon eigenvalues through the whole high-symmetry points as presented in Fig. 2(a), indicating the dynamical stability of free-standing  $\text{Ge}_3\text{N}_4$  in its ground-state structure. The total 42 phonon branches of single-layer  $\text{Ge}_3\text{N}_4$  include 13 doubly-degenerate and 13 non-degenerate optical branches as a result of the  $P-3$  space symmetry of the structure. The highest frequency optical phonon branch is found to have a frequency of  $869\text{ cm}^{-1}$  at the  $\Gamma$  point, which is much lower than that of BN, in contrast, larger than those for AlN, GaN, and InN indicating quite stronger Ge-N bonds in  $\text{Ge}_3\text{N}_4$  [57].

The Raman activities of  $\Gamma$ -centered phonon modes are investigated by means of first-order off-resonant Raman calculations, which is suitable for the characterization of the material. As presented in Fig. 2(a) (right-panel), totally 13 optical branches are found to be Raman active. Among the 13 Raman active modes, we characterize the most prominent 8 phonon modes in terms of their atomic vibrations. The illustrated vibrational motions (see Fig. 2b) reveal that 4 of the Raman active modes correspond to purely in-plane while 2 of them arise from the out-of-plane vibrations of the atoms. In addition, there are also 2 Raman active modes which consist of coupled in-plane and out-of-plane

vibrations. The Raman modes having in-plane vibrational character have frequencies of  $223.5$ ,  $390.8$ ,  $611.0$ , and  $850.7\text{ cm}^{-1}$ . The phonon modes at frequencies  $850.7$  and  $390.8\text{ cm}^{-1}$  are dominated by the vibrations of the inner N atoms, while the peak at  $611.0\text{ cm}^{-1}$  mainly arises from vibration of the outer N atoms. Moreover, the lowest frequency in-plane mode (at  $235.5\text{ cm}^{-1}$ ) stands for the rotational motion of neighboring Ge groups. On the other hand, among the out-of-plane Raman active vibrations, the peak at  $589.2\text{ cm}^{-1}$  arises from pure outer N oscillations. In contrast, the phonon mode having frequency of  $372.9\text{ cm}^{-1}$  is dominated by the inner N vibrations with slightly weak contribution of outer N atoms. Furthermore, the Raman active modes at  $320.0$  and  $462.7\text{ cm}^{-1}$  correspond to the coupled vibrations of Ge (in-plane) and N (out-of-plane) atoms vibrations. For further analysis of the atomic contributions to the phonon vibrations, the partial phonon density of states are calculated (see Fig. S3 in Supplementary Information). Similar to the atomic weight factors calculated by Chen et al. [62], atomic-based phonon density of states give information about the atomic contributions to the vibrations. Apparently, the phonon modes below the frequency  $300\text{ cm}^{-1}$  are dominated by the Ge-vibrations while the optical phonons above  $300\text{ cm}^{-1}$  mostly arise from N-vibrations. The analysis of the Raman spectrum of single-layer  $\text{Ge}_3\text{N}_4$  provide deep analysis about the characteristic of its structure.

### 3.3. Electronic Properties

Electronic properties of single-layer  $\text{Ge}_3\text{N}_4$  are investigated in terms of the electronic band dispersions. As shown in Fig. 3, the valence band maximum (VBM) resides between the  $\Gamma$ -M points of the Brillouin Zone while the conduction band minimum (CBM) is located at the  $\Gamma$  point, indicating the indirect band gap nature of single-layer  $\text{Ge}_3\text{N}_4$ . The electronic band dispersions reveal that the top valence states are only dispersive around the  $\Gamma$  point while they are mostly localized through the M-K points. The electronic band gap is calculated to be  $3.27\text{ eV}$ . As compared to the predicted electronic band gaps of  $\alpha$ -,  $\beta$ -, and  $\gamma$ - $\text{Ge}_3\text{N}_4$  phases ( $3.85\text{ eV}$ ,  $3.86\text{ eV}$  and  $3.56\text{ eV}$ , respectively), single-layer  $\text{Ge}_3\text{N}_4$  possesses a slightly smaller band gap [12]. In addition, the electronic band gap of single-layer  $\text{Ge}_3\text{N}_4$  is much smaller than the experimentally observed band gap of  $\gamma$ - $\text{Ge}_3\text{N}_4$  ( $4.50\text{ eV}$ ) [5]. It is seen that the dimensional reduction from bulk to 2D structure results in the decrease of the electronic band gap. Moreover, the work function of the predicted single-layer  $\text{Ge}_3\text{N}_4$  is calculated to be  $6.38\text{ eV}$  which is much larger than those for single-layers of  $\text{MoS}_2$  ( $5.10\text{ eV}$ ) and  $h\text{-BN}$  ( $4.70\text{ eV}$ ) [40]. Apparently, the higher work function of single-layer  $\text{Ge}_3\text{N}_4$  indicates the localized characteristics of the electron at the top valence state. (see Table 1).

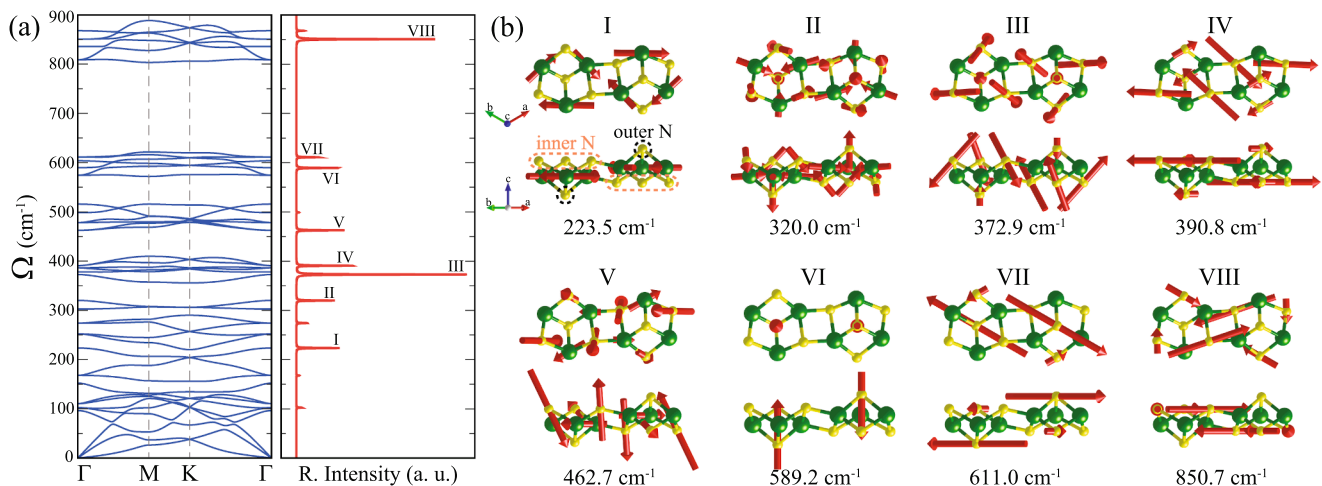
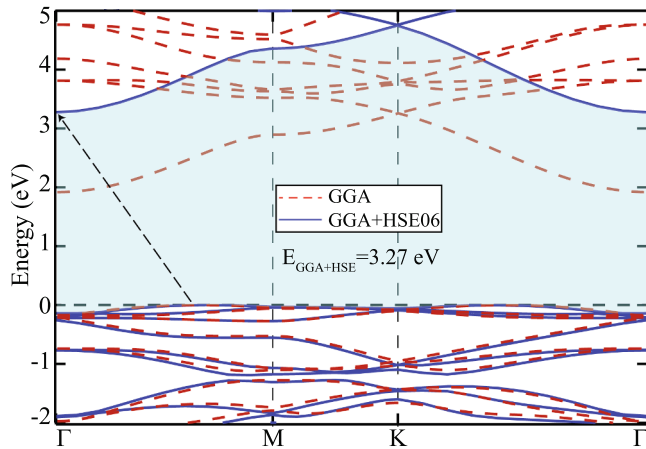


Fig. 2. For the single-layer of  $\text{Ge}_3\text{N}_4$ ; (a) predicted phonon band structure (left panel) and the corresponding Raman activity of zone-centered vibrations (right panel). (b) Illustrated atomic vibrations of various Raman active phonon modes.



**Fig. 3.** Electronic band structure of single-layer  $\text{Ge}_3\text{N}_4$ . Red dashed lines belong to bare GGA band structure while blue lines represent band structure calculated with GGA + HSE06.

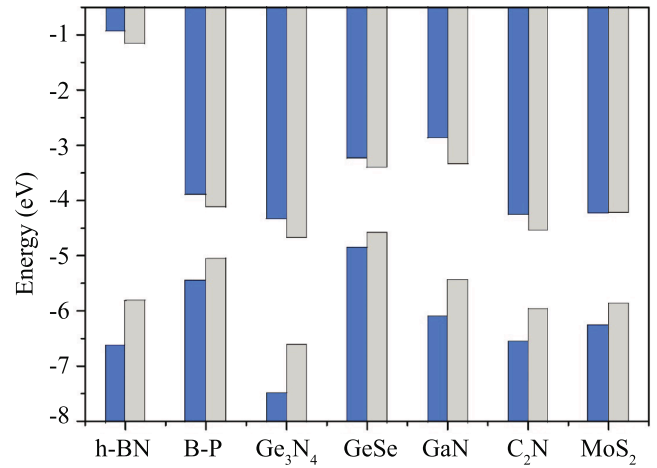
Experimental studies have demonstrated that single-layer 2D materials can be used as the building blocks for the formation of van der Waals type heterostructures in order to combine their electronic properties in a single 2D structure. Fig. 4 shows the band alignment of single-layer  $\text{Ge}_3\text{N}_4$  with several typical 2D single-layers. As shown in Fig. 4, the vacuum level of each single-layer is set to zero energy. After the shift of band edge energies by the vacuum energy, the CBM and VBM energies of  $\text{Ge}_3\text{N}_4$  are found to be  $-4.33$  and  $-7.49$  eV from HSE06, and  $-4.69$  and  $-6.6$  eV from PBE, respectively. In order to make a general conclusion, various single-layer materials from different 2D groups are considered.  $\text{MoS}_2$ , a famous member of TMDs,  $\text{GeSe}$  and  $\text{B-P}$  are chosen as the non-planar single-layers while graphene-like planar structures of  $h\text{-BN}$ ,  $\text{GaN}$ , and  $\text{C}_2\text{N}$  are considered as one-atom-thick materials. It is seen that the VBM energy of single-layer  $\text{Ge}_3\text{N}_4$  is lower than that of other 2D materials considered in our study. Note that while the band gap energy of each single-layer changes with the inclusion of HSE06 in the calculations, the type of the band alignment is not affected by the functional. As shown in Fig. 4, single-layer  $\text{Ge}_3\text{N}_4$  is predicted to form type-II band alignment with all 2D materials except for single-layer  $\text{GeSe}$  whose VBM and CBM energies are higher than those of  $\text{Ge}_3\text{N}_4$ . This facilitates the separation of electron and holes in van der Waals heterostructures constructed by  $\text{Ge}_3\text{N}_4$  and these 2D materials, with electron localized on the  $\text{Ge}_3\text{N}_4$  layer and hole localized on the other layer. In contrast, the  $\text{GeSe-Ge}_3\text{N}_4$  heterostructure forms a type-I band alignment in which both electron and hole are localized on single-layer  $\text{Ge}_3\text{N}_4$ .

### 3.4. Strain-dependent properties

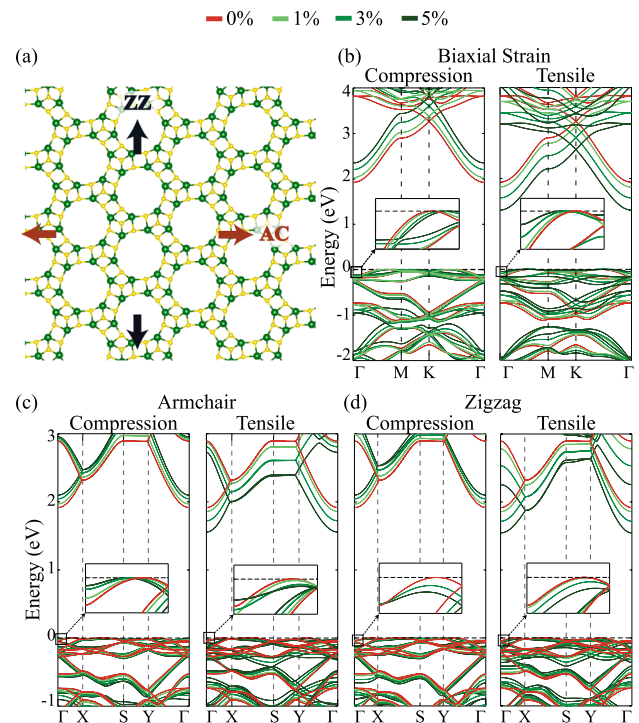
Strain is often present in experiments occurring either naturally or controllably and it can alter the electronic properties of materials. Since it is an easy and effective method, strain has often been used to manipulate fundamental properties of ultra-thin materials [63,64]. In the present section, we present our results on how the electronic structure of single-layer  $\text{Ge}_3\text{N}_4$  responds against applied uniaxial and biaxial strains. For the investigation of uniaxial strain effect, a rectangular unit cell containing 28-atoms is constructed in order to simulate the strain

along the two main orientations in the lattice, namely zigzag (ZZ) and armchair (AC) directions (see Fig. 5(a)).

Effects of uniaxial as well as biaxial strains on the electronic band



**Fig. 4.** Band alignment between  $\text{Ge}_3\text{N}_4$  and several typical 2D materials. Blue and gray bars indicate results calculated by HSE06 and PBE, respectively. The vacuum energy is set as zero.



**Fig. 5.** (a) AC and ZZ orientations of single-layer  $\text{Ge}_3\text{N}_4$  with rectangular unit cell. The electronic band diagrams of single-layer  $\text{Ge}_3\text{N}_4$  under (b) biaxial strain, (c) uniaxial strain on AC orientation, (d) uniaxial strain on ZZ orientation.

**Table 1**

For the single-layer of  $\text{G}_3\text{N}_4$ ; optimized in-plane lattice parameter,  $a$ ; the vertical distance between the outer-most N atoms,  $h$ ; the amount of charge donated by a Ge atom and received by a N atom,  $\rho_{\text{Ge}}$  and  $\rho_{\text{N}}$ ; the work function,  $\phi$ ; calculated cohesive energy per atom,  $E_{\text{Coh}}$ ; electronic band gaps calculated within GGA and HSE06 functionals,  $E_{\text{Gap}}$  and  $E_{\text{Gap}}^{\text{HSE06}}$ ; and the linear-elastic parameters, in-plane stiffness ( $C$ ) and Poisson ratio ( $\nu$ ).

	$a$	$h$	$\rho_{\text{Ge}}$	$\rho_{\text{N}}$	$\phi$	$E_{\text{Coh}}$	$E_{\text{Gap}}$	$E_{\text{Gap}}^{\text{HSE06}}$	$C$	$\nu$
	(Å)	(Å)	( $e^-$ )	( $e^-$ )	(eV)	(eV/atom)	(eV)	(eV)	(N/m)	-
$\text{Ge}_3\text{N}_4$	8.16	2.79	1.8	1.3	6.38	4.08	1.92	3.27	62	0.24

dispersions are calculated by changing the lattice parameters by  $\pm 1\%$ ,  $\pm 3\%$  and  $\pm 5\%$  amounts both in tensile and compressive cases. The results for the biaxial strain are presented in Fig. 5(b). It is seen that the CBM of single-layer  $\text{Ge}_3\text{N}_4$  displays shift to lower energies via applied tensile biaxial strain while it shifts to higher energies under compressive strain. As a result of those shifts of the CBM, the electronic band gap is found to change from 1.30 eV (at 5% of tensile biaxial strain) to 2.34 eV (at 5% of compressive biaxial strain). Note that the indirect gap behavior of  $\text{Ge}_3\text{N}_4$  is robust against the applied biaxial strain regardless of the strain type, compressive or tensile. In addition, while the location of VBM does not change via biaxial strain, the energy of the valence states at the  $\Gamma$  point increases under tensile strain resulting in less dispersive states residing between the  $\Gamma$ -M points.

On the other hand, our results for the applied uniaxial strains are shown in Figs. 5(c) and (d) (for AC and ZZ directions, respectively). Note that since a rectangular cell is used for the uniaxial strain, the high symmetry points are given in the corresponding frame. For the applied strain types and strain ranges, the obtained stress-strain curves (see Fig. S2 of Supplementary Information) reveal that the structures fall into elastic limits in terms of their elastic stabilities. Therefore, the applied strain strengths are meaningful such that the structures do not undergo an elastic deformation. It is seen that regardless of the strain direction, the energy of the CBM displays a shift to higher (lower) energies via applied compressive (tensile) strain. However, in all cases the CBM resides at the same point under applied uniaxial strain. As zoomed out in the insets of Figs. 5(c) and (d), the compressive uniaxial strain along AC direction exhibits a similar effect with that of tensile biaxial strain for the valence state residing between the  $\Gamma$ -M points. It is found that the electronic band gap decreases (increases) via uniaxial tensile (compressive) strains. The energy band gap ranges from 1.56 eV (at 5% of tensile uniaxial strain) to 2.10 eV (at 5% of compressive uniaxial strain) in both directions. It is clear that the indirect nature of the electronic band gap is not affected by the type or direction of the uniaxial strain while the band gap changes depending on the strength of the strain. The mechanism behind such change can be found in the atomic orbital contributions to the lowest conduction and highest valence states. It is found that the CBM state is formed by the in-plane orbitals of the atoms, which indicates that those states are more sensitive to the applied in-plane strain. In contrast, the VBM state is dominated by the out-of-plane orbitals of the individual atoms and thus, VBM is mostly unaffected by the in-plane strain.

#### 4. Conclusions

In summary, we performed DFT-based first-principles calculations in order to investigate the structural, vibrational and electronic properties of single-layer  $\text{Ge}_3\text{N}_4$  and the effects of biaxial and uniaxial strains on the electronic properties were reported. Geometry optimization revealed that single-layer  $\text{Ge}_3\text{N}_4$  possesses a holey buckled structure. Phonon band dispersion calculations showed that single-layer  $\text{Ge}_3\text{N}_4$  is dynamically stable. Further investigations on vibrational properties indicated that Raman active phonon modes can be used as key for the identification of single-layer  $\text{Ge}_3\text{N}_4$  via Raman spectroscopy. Moreover, the electronic properties of single-layer  $\text{Ge}_3\text{N}_4$  were investigated in terms of the electronic bands and it was shown that  $\text{Ge}_3\text{N}_4$  is a large gap semiconductor with an indirect band gap behavior. In addition, it was also predicted that single-layer  $\text{Ge}_3\text{N}_4$  forms type-II vdW heterostructures with various one-atom-thick and puckered 2D materials except for single-layer GeSe which gives rise to a type-I band alignment. Furthermore, it was found that independent of the type of the applied strain, biaxial or uniaxial, single-layer  $\text{Ge}_3\text{N}_4$  preserves its indirect gap nature while its electronic band gap is tunable with external strain. Single-layer  $\text{Ge}_3\text{N}_4$  can be considered as a potential candidate for nanoelectronic applications with its strain-tunable band gap.

#### Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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#### Appendix A. Supplementary material

Supplementary data associated with this article can be found, in the online version, at <https://doi.org/10.1016/j.apsusc.2021.151361>.

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